

## **A JOINT MODEL OF WEEKEND DISCRETIONARY ACTIVITY PARTICIPATION AND EPISODE DURATION**

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## **ABSTRACT**

Research on travel demand modeling has primarily focused on weekday activity-travel patterns. However, weekend activities and travel constitute a major component of individuals' overall weekly activity-travel participation. This paper describes a modeling effort that focuses on discretionary-event weekend activity-travel demand. This study bridges the gap in the literature by modeling discretionary event type participation, duration of participation, and accompaniment type jointly in a simultaneous equations model system. A joint discrete-continuous modeling framework is formulated for analyzing these dimensions as a choice bundle. Specifically, the combination of event type and accompaniment type constitutes the discrete component while the duration of participation constitutes the continuous component. The model employs a copula-based sample selection approach that ties the discrete choice error component with the duration error component in a flexible manner. The data used in the paper is drawn from the 2008-2009 National Household Travel Survey sample of the Greater Phoenix metropolitan area in Arizona. The results from the estimation process clearly highlight the presence of sample selection in the joint modeling context. Furthermore, the results also highlight the flexibility of copula models in capturing such sample selection. The best copula model results were employed to generate hazard profiles for various alternative related duration intervals. The profiles generated highlight the inaccurate predictions obtained using approaches that ignore the presence of sample selection.

*Keywords:* Weekend activity participation, Sample selection, Copula, Duration modeling, Hazard profiles

## 1. INTRODUCTION

Research on travel demand modeling has primarily focused on weekday activity-travel patterns. However, weekend activities and travel constitute a major component of individuals' overall weekly activity-travel participation. Recent studies suggest that the level of weekend and weekday personal travel (both in terms of number of trips and person miles of travel) are about the same, and that the levels of mid-day weekend traffic congestion almost reach weekday commute traffic congestion levels in some locations (1). This is not surprising, as discretionary special events (such as exhibitions, sporting events, and concerts) are more likely to be held over the weekend, leading to congestion in and around the discretionary special event sites. As cities move toward increasing weekend social, recreational, and cultural opportunities, it is important to understand and forecast the resulting weekend activity-travel patterns. The analysis of weekend activity-travel patterns is also important from the standpoint of policy analysis. For instance, there is evidence that individuals move activities to the weekend when their weekday schedules get busy or when traffic congestion during the commute periods leaves too little time for weekday discretionary activity participation (2,3).

Overall, whether for demand forecasting or for analyzing the effects of transportation-related policy actions, it is important to examine special event-related weekend activity-travel patterns. In doing so, there are several key characteristics of weekend activity-travel patterns worthy of explicit recognition: (1) weekend activity-travel is highly leisure-oriented, (2) weekend activities may not have the same level of spatial and temporal rigidity as work activities (although some activities such as ballgames, church activities, and special events may have fixed locations and schedules), (3) inter-personal interactions in activity participation are stronger on the weekends due to greater joint activity participation and travel, and (4) the activity travel environment differs substantially between weekdays and weekends (for example, differences in facility operating hours, and lower transit level-of-service) (4).

The current study augments the literature on weekend activity participation by modeling (1) discretionary special event type participation, (2) duration of participation and (3) accompaniment type (i.e., the travel party composition for the activity). The data used in the paper is drawn from the 2008-2009 National Household Travel Survey (NHTS) conducted in the United States. The survey sample residing in the Greater Phoenix metropolitan region in Arizona is extracted for use in this study. The study employs a copula-based joint discrete-continuous model of weekend activity participation to address the different dimensions involved in special event activity participation.

The rest of the paper is organized as follows. Section 2 provides a review of earlier literature on weekend activity participation while positioning the current study. In section 3, the methodology employed in the paper is outlined. Section 4 describes the data assembly process. Section 5 presents estimation results. Section 6 summarizes the paper and offers directions for future research in this arena.

## 2. EARLIER RESEARCH AND THE FOCUS OF THE CURRENT PAPER

Weekend activity participation and time-use has been receiving increased attention in the transportation field. These research efforts may be broadly classified into two categories: (1) studies that focus on comparison between weekend and weekday activity participation and (2) studies that exclusively examine weekend activity participation.

In the first category of studies, Bhat and Misra (5), Yamamoto and Kitamura (6) and Truth, et al. (7), examine the allocation of time for discretionary activities on weekend days and

weekdays while Sugie et al. (8) examine the interdependency of shopping activity participation on weekday and weekend days. Some studies present comprehensive exploratory analysis of the comparison between weekday and weekend activity-travel patterns (4), while other studies highlight the differences in joint activity participation patterns between weekdays and weekend days (9). There has also been recent work applying time use models to study activity participation differences across weekdays and weekends; for example Lee et al. (3) compared how weekday and weekend maintenance and discretionary activity time-use are affected by land-use and transportation network characteristics using multiple equation tobit models. For example, they found that in locations with suburban type density, individuals tend to lump discretionary activities for the weekends. Finally, some recent studies employ duration modeling approaches to study the differences between weekday and weekend activity patterns (see Zhong et al. (10) for separate duration models for various activity types). In summary, these studies highlight that weekday and weekend activity behavior differ in terms of activities pursued, activity duration (longer discretionary activity participation during weekends) and the activity travel environment experienced.

The second category of studies focuses exclusively on weekend participation. Bhat and Gossen (2) examined weekend activity and travel participation considering in-home and out-of-home activities, and worker and non-worker activity-travel patterns. Bhat et al. (11) examine individual activity time-use participation in maintenance and leisure activities over the weekend. Kapur and Bhat (12) use the American Time Use Survey to examine weekend discretionary activity participation patterns in terms of the “with whom” dimension (household and non-household members). Sall and Bhat (1) examined the spatial and temporal characteristics of weekend work episodes. Zhong and Hunt (13) proposed a duration model of weekend activity participation by different activity types. Habib (14) formulated a random utility based approach to examine weekend activity participation and scheduling. These studies underscore the importance of socio-demographics, urban built environment, weekend day effects and seasonal effects on weekend activity participation. Despite the recognition of the role of weekend activity-travel patterns in travel demand analysis and greenhouse gas emissions, there are virtually no research efforts focused on examining factors influencing discretionary special event activity participation, duration, and accompaniment type for the event (15). The importance of modeling activity duration and accompaniment type dimensions has been noted in the literature (e.g., Kato and Matsumoto (16); Bhat (17)). Activity durations are directly related to vehicle soak times for automobile users - an important variable for emissions estimation. The accompaniment type strongly influences travel mode choice (and vehicle type choice for auto trips), choice dimensions with important energy and environmental implications.

More recently, studies have explored the impact of social networks (such as personal contacts/networks) on various characteristics of discretionary activity participation (see (18, 19, 20, 21)). These studies relate the propensity for discretionary activity participation to individual’s social network characteristics such as network composition and structure. While these studies provide an improved understanding of the determinants of discretionary activity participation, they generally require specialized data collection efforts. Typical travel diary based data sets do not compile such detailed information making it difficult to apply the proposed frameworks to study discretionary special event participation decisions.

This study bridges the gap in the literature by modeling (1) discretionary event type participation, (2) duration of participation, and (3) accompaniment type (i.e., with whom the individual participates in the special event). Our intent in this paper is to develop and exercise a

framework that can be estimated using traditional travel diary data sets currently compiled by urban metropolitan agencies. The study presents a joint discrete-continuous framework for analyzing these dimensions. Specifically, the combination of event type and accompaniment type constitutes the discrete component while the duration of participation constitutes the continuous component. The discrete framework is quite appropriate in the current context because only a very small fraction of individuals pursue multiple discretionary special events within the same weekend day.

In terms of the continuous choice, the duration of the event for a particular discrete alternative is observed only if participation has occurred, necessitating the consideration of self-selection in the model structure. A copula-based sample selection approach that ties the discrete choice error component with the duration error component in a flexible manner is adopted in this study to account for this. In particular, the copula approach allows the testing of several flexible dependence structures rather than pre-imposing restrictive distributional assumptions (see Bhat and Eluru (22) for an extensive discussion of the copula approach). The methodological details of the copula-based discrete-continuous model are presented in the next section.

### 3. METHODOLOGY

In this section, the structure of the copula-based joint generalized extreme value duration framework to jointly model weekend event type choice, accompaniment type choice, and activity duration is presented. The weekend event type and accompaniment type choice component takes the form of a generalized extreme value model while the event duration component takes the form of a non-parametric proportional hazard duration model. In addition to allowing a flexible parametric hazard distribution, the non-parametric duration model is ideally suited for hazard model estimation in the context of interval-level reporting of duration (where respondents round their activity and travel start and end times to the nearest five or 10 minutes when responding to travel or time use surveys).

#### 3.1. Model Structure

The modeling of event type and company type choice is undertaken using a generalized extreme value framework. Specifically, let  $q$  be the index for individuals and let  $i$  be the index for the discrete choice combination of event type and company type. Also, let  $h_{qi}^*$  be the latent (indirect) utility accrued by individual  $q$  from participation in alternative  $i$ . Without any loss of generality, let  $i=1$  represent the discrete category that corresponds to non-participation in any out-of-home event type. Then, write:

$$h_{qi}^* = \beta' x_{qi} + \varepsilon_{qi}, \quad (1)$$

where  $x_{qi}$  is a vector of independent variables,  $\beta$  is a corresponding vector of coefficients to be estimated, and  $\varepsilon_{qi}$  represents an idiosyncratic error term. Assume that the  $\varepsilon_{qi}$  terms are identically and independently Gumbel distributed across outcomes  $i$  and individuals  $q$  with a location parameter equal to 0 and a scale parameter equal to 1.<sup>1</sup> Individual  $q$  participates in alternative  $i$  if, and only if,

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<sup>1</sup> The methodology is also applicable to generalized GEV structures for the error terms. In fact, this is what we have done in our analysis and code. However, as we will discuss later, in the empirical context of the current paper, the discrete choice model consistently collapsed to the multinomial logit model for a whole range of variable

$$h_{qi}^* > \max_{\substack{j=1,2,\dots,I \\ j \neq i}} h_{qj}^* \quad (2)$$

Let  $r_{qi}$  be a dichotomous variable;  $r_{qi} = 1$  if the  $i$ th alternative is chosen by the  $q$ th individual, and  $r_{qi} = 0$  otherwise. Defining

$$v_{qi} = \varepsilon_{qi} - \left\{ \max_{j=1,2,\dots,I, j \neq i} h_{qj}^* \right\}, \quad (3)$$

and substituting the right side for  $h_{qi}^*$  from Equation (1) in Equation (2), it is possible to write:

$$r_{qi} = 1 \text{ if and only if } \beta' x_{qi} + v_{qi} > 0 \quad (4)$$

The implied marginal distribution of  $v_{qi}$  can be obtained from Equation (3) and from the distributional assumptions on the  $\varepsilon_{qi}$ 's as follows:

$$F_i(v) = \text{Prob}(v_{qi} < v) = \frac{\sum_{j \neq i} \exp(\beta' z_{qj})}{\exp(-v) + \sum_{j \neq i} \exp(\beta' z_{qj})}, \quad i = 1, 2, \dots, I. \quad (5)$$

Next, let  $s_{qi}$  represent the (continuous) duration time of participation in alternative  $i$  ( $i=2,3,\dots,I$ ) for individual  $q$ . The hazard function for individual  $q$ 's duration in alternative  $i$  at some specified time  $t$  on the continuous-time scale  $T$ ,  $\lambda_{qi}(t)$ , is defined using the proportional hazard specification as (23):

$$\lambda_{qi}(t) = \lim_{\delta \rightarrow 0^+} \frac{\text{prob}[t + \delta > s_{qi} \geq t \mid s_{qi} \geq a]}{\delta} = \lambda_{0i}(t) \exp(-\gamma' z_{qi}), \quad (6)$$

where  $\lambda_{0i}(t)$  is the continuous-time baseline hazard at time  $t$  for special event type  $i$ ,  $z_{qi}$  is a column vector of covariates for individual  $q$  and alternative  $i$ , and  $\gamma$  is a column vector of parameters to be estimated.<sup>2</sup> Equation (6) can be written in the equivalent form (17),

$$s_{qi}^* = \ln \Lambda_{0i}(s_{qi}) = \gamma' z_{qi} + \eta_{qi}, \quad (7)$$

where  $\Lambda_{0i}(\cdot)$  is the integrated baseline hazard for alternative  $i$  ( $i=2,3,\dots,I$ ) and  $\eta_{qi}$  takes an extreme value form with distribution function given by:<sup>3</sup>

$$\Pr(\eta_{qi} < \eta) = G(\eta) = 1 - \exp[-\exp(\eta)] \quad (8)$$

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specifications. Thus, to keep the presentation simple in this methodology section, we consider the error terms to be identically and independently distributed. Readers interested in getting the details of the more general methodology may obtain this by contacting the corresponding author.

<sup>2</sup>  $\lambda_{0i}(t)$  may be viewed as the instantaneous probability that individual  $q$ 's duration in event type  $i$  will be terminated in an infinitesimal time interval beyond time point  $t$ , given that the duration did not terminate before time point  $t$ .

<sup>3</sup> The distribution form is the same across event type regimes  $i$  ( $i=2,3,\dots,I$ ), and hence the function  $G$  is not subscripted by the index  $i$  in the equation below.

The dependent variable in Equation (7) is a continuous unobserved variable when duration data are available only in grouped form. However, the time interval of activity participation,  $t_{qi}$ , for individual  $q$ 's chosen alternative  $i$  ( $i=2,3,\dots,I$ ) is observed. Let the time intervals be represented by an index  $k$  ( $k=1,2,3,\dots,K$ ), with these time intervals being related to the continuous time dimension  $T$  in terms of bounds on the continuous time scale:  $k=1$  if  $T \in [0, T_1]$ ,  $k=2$  if  $T \in [T_1, T_2]$ , ...,  $k=K$  if  $T \in [T_{K-1}, \infty]$  (the duration interval cut off points can be different for different alternatives; however, for ease in notation, they are assumed to be the same for all alternatives). Thus,  $t_{qi} = k$  if the duration spell of individual  $q$  ends in time interval  $k$  for the chosen alternative  $i$  ( $i=2,3,\dots,I$ ).

The overall equation system for the joint choice of discretionary event-accompaniment type discrete choice combination and duration can be written from Equations (1) through (7) as:

$$\begin{aligned} r_{qi}^* &= \beta' x_{qi} + v_{qi}, \quad r_{qi} = 1 \text{ if } r_{qi}^* > 0, \quad r_{qi} = 0 \text{ otherwise} \\ s_{qi}^* &= \gamma' z_{qi} + \eta_{qi}, \quad t_{qi} = k \text{ if } \delta_{i,k-1} < s_{qi}^* \leq \delta_{i,k}, \\ t_{qi} &\text{ observed only if } r_{qi} = 1 \text{ (} i=2,3,\dots,I \text{)}, \quad \delta_{i,k} = \ln \Lambda_{0i}(T^k) \end{aligned} \quad (9)$$

In the above equation system,  $\delta_{i,0} = -\infty$  and  $\delta_{i,K} = +\infty$  for each alternative  $i$  ( $i=2,3,\dots,I$ ). The probability that an individual  $q$  will choose alternative  $i$  ( $i=2,3,\dots,I$ ) and participate for a grouped duration interval of  $k$  may be written as follows:

$$\begin{aligned} \Pr[r_{qi} = 1, t_{qi} = k] &= \Pr[v_{qi} > -\beta' x_{qi}, \delta_{i,k-1} - \gamma' z_{qi} < \eta_{qi} < \delta_{i,k} - \gamma' z_{qi}] \\ &= \Pr[\delta_{i,k-1} - \gamma' z_{qi} < \eta_{qi} < \delta_{i,k} - \gamma' z_{qi}] - \Pr[v_{qi} < -\beta' x_{qi}, \delta_{i,k-1} - \gamma' z_{qi} < \eta_{qi} < \delta_{i,k} - \gamma' z_{qi}] \\ &= G(\delta_{i,k} - \gamma' z_{qi}) - G(\delta_{i,k-1} - \gamma' z_{qi}) - \\ &\quad \left( \Pr[v_{qi} < -\beta' x_{qi}, \eta_{qi} < \delta_{i,k} - \gamma' z_{qi}] - \Pr[v_{qi} < -\beta' x_{qi}, \eta_{qi} < \delta_{i,k-1} - \gamma' z_{qi}] \right) \end{aligned} \quad (10)$$

The above probability depends upon the dependence structure between the random variables  $v_{qi}$  and  $\eta_{qi}$  for each special event type  $i$ . In the duration context of interest in this paper, Bhat (24) proposed the use of Lee's sample selection method (25) for this coupling, which essentially corresponds to the use of a Gaussian copula (22). However, this approach imposes the restriction that the dependence surface is linear and symmetric. There is no reason to believe that such a Gaussian coupling is appropriate. In particular, it is important to test different parametric functional forms for this bivariate dependency surface and pick the one that empirically fits the data best. Recent developments related to copula techniques provide an effective way to do so.

### 3.2. General Bivariate Copula Structure

A copula is a device or function that generates a stochastic dependence relationship (i.e., a multivariate distribution) among random variables with pre-specified marginal distributions (see Bhat and Eluru (22); Trivedi and Zimmer (26)). The precise definition of a copula is that it is a multivariate distribution function defined over the unit cube linking uniformly distributed marginals. In the bivariate case, let  $C$  be a 2-dimensional copula of uniformly distributed random variables  $U_1$  and  $U_2$  with support contained in  $[0,1]$ . Then,

$$C_{\theta}(u_1, u_2) = \Pr(U_1 < u_1, U_2 < u_2), \quad (11)$$

where  $\theta$  is a parameter of the copula commonly referred to as the dependence parameter. A copula, once developed, allows the generation of joint bivariate distribution functions with given

marginals. Thus, a bivariate distribution  $J_i(v, \eta)$  can be generated for the two random variables  $v_{qi}$  (with margin  $F_i$ ) and  $\eta_{qi}$  (with margin  $G$ ) using the following expression (see Sklar (27)):

$$J_i(v, \eta) = \Pr(v_{qi} < v, \eta_{qi} < \eta) = \Pr[U_1 < F_i(v), U_2 < G(\eta)] = C_\theta[u_1 = F_i(v), u_2 = G(\eta)] \quad (12)$$

A rich set of bivariate copulas  $C_\theta(u_1, u_2)$  are available, including the Gaussian copula, the Farlie-Gumbel-Morgenstern (FGM) copula, and the Archimedean class of copulas (including the Clayton, Gumbel, Frank, and Joe copulas). For given functional forms of the margins, the precise bivariate dependence profile between the variables  $v_{qi}$  and  $\eta_{qi}$  is a function of the copula  $C_\theta(u_1, u_2)$  used, and the dependence parameter  $\theta$ . For detailed descriptions of the alternative copulas and their formulations, please see Bhat and Eluru (22).

### 3.3. Estimation Procedure

The parameters to be estimated in the joint discrete-duration model include the  $\beta$  vector, the  $(K-1)$   $\delta_{i,k}$  parameters ( $\delta_{i,0} = -\infty$  and  $\delta_{i,K} = +\infty$ ) for each event type  $i$  ( $i=2,3,\dots,I$ ), and the vector  $\gamma$ . From Equation (1), the probability of an individual choosing not to participate in any event type is simply the generalized extreme value probability expression; for example if the  $\varepsilon_{qi}$  error terms are assumed to be independent across discrete alternatives then the probability is given below:

$$\text{Prob}(r_{q1} = 1) = \frac{\exp(\beta' z_{q1})}{\sum_j \exp(\beta' z_{qj})}, \quad j = 1, 2, \dots, I. \quad (13)$$

If some other GEV form is used for the  $\varepsilon_{qi}$  terms, then the implied distribution of  $v_{qi}$  will take the corresponding GEV probability form. In this paper, the multinomial logit and nested logit structures were examined. The probability of an individual choosing discrete choice combination  $i$  ( $i=2,3,\dots,I$ ) and a duration interval  $k$  may be obtained from Equation (10) and the appropriate copula expression as:

$$\text{Prob}[r_{qi} = 1, t_{qi} = k] = G(\delta_{i,k} - \gamma' z_{qi}) - G(\delta_{i,k-1} - \gamma' z_{qi}) - [C_\theta(u_{qi1}, u_{qi,k,2}) - C_\theta(u_{qi1}, u_{qi,k-1,2})], \quad (14)$$

where  $u_{qi1} = F_i(-\beta' x_{qi})$  and  $u_{qi,k,2} = G(\delta_k - \gamma' z_{qi})$ .

The corresponding probability for the original Lee's transformation will be slightly different and is given by:

$$\text{Prob}[r_{qi} = 1, t_{qi} = k] = [C_\theta(u_{qi1}, u_{qi,k,2}) - C_\theta(u_{qi1}, u_{qi,k-1,2})], \quad (15)$$

where  $u_{qi1} = F_i(\beta' x_{qi})$  and  $u_{qi,k,2} = G(\delta_k - \gamma' z_{qi})$ .

Next, let  $I[\cdot]$  be an indicator function taking the value of unity if the expression in parenthesis is true and 0 otherwise. Also, define the following dummy variables for  $i=2,3,\dots,I$ :

$$M_{qik} = I[r_{qi} = 1] \times I[t_{qi} = k]. \quad (16)$$

Then, the log likelihood function for the copula model takes the form

$$\log L = \sum_{q=1}^Q \left( r_{q1} \log[\text{Prob}(r_{q1} = 1)] + \sum_{i=2}^I \sum_{k=1}^K M_{qki} \log [\text{Prob}(r_{qi} = 1, t_{qi} = k)] \right) \quad (17)$$

All of the parameters in the model are consistently estimated by maximizing the log-likelihood function, which is accomplished using the GAUSS matrix programming language. Once the threshold parameters ( $\delta_{i,k}$  parameters) are estimated for each alternative, the baseline hazard for discrete period  $k$  and alternative  $i$  ( $i=1,2,\dots,I$ ),  $\lambda_{0i}^*(k)$ , can be computed using the expression below:

$$\lambda_{0i}^*(k) = \frac{G(\delta_{i,k}) - G(\delta_{i,k-1})}{1 - G(\delta_{i,k-1})} \quad (18)$$

#### 4. DATA

The data used in this study is derived from the 2008-2009 National Household Travel Survey (NHTS) in the United States. The data set used for this study corresponds to survey records from the Greater Phoenix metropolitan area. The MAG add-on sample included more than 4,400 households who provided detailed socio-economic, demographic, and personal travel information (for a 24 hour travel diary period). The households were evenly distributed across the days of the week, such that about 2/7<sup>th</sup> of the 4,400 households responded to the survey and reported their trips for a weekend day (Saturday or Sunday).

The analysis in this paper is restricted to activity-travel participation on weekends for individuals 14 years of age or older. Four different discretionary event activity types are considered:

- Social/recreational activity
- Visit friends/family
- Go out/hang out
- Visit public place

As an individual may choose to participate in any combination of these activities over the course of a weekend day, discrete alternatives are constructed by considering all possible combinations of activity engagement. This leads to a total of  $2^4 - 1 = 15$  alternatives. In addition to these activity alternatives, three accompaniment options are defined:

- Alone
- With household members only
- With non-household members (may or may not include household members)

By crossing the 15 activity type participation alternatives with the three accompaniment type options, a total of 45 alternatives are obtained for the discrete component of the model system. Thus an individual may participate in multiple discretionary activity events, but cannot mix and match accompaniment types across the discretionary events. For example, a person who pursues social recreation alone and visits a public place alone would be included (because that person's choice appears within the 45 elemental choice set). However a person who pursues social recreation alone and visits a public place with household members would not be included in the analysis. This definition of the choice set is not too restrictive because the percent of individuals (responding to the survey on a weekend day) who engaged in multiple discretionary activity events with differing accompaniment types is extremely small at just over two percent of the sample. Thus, the choice set definition adopted in this study accounts for nearly 98 percent of the weekend

survey respondents. The 46<sup>th</sup> and final alternative is the choice to not engage in any discretionary activity event.

After extensive cleaning and data preparation, the final sample used for model estimation included 1773 individuals, 481 of whom made at least one discretionary event on the weekend day. The other individuals engaged in absolutely no special discretionary activity event (they may have done other activities, but they did not engage in the four specific activities of interest in this paper). Table 1 offers a detailed description of the discretionary activity participation and duration for the survey sample. It is found that 9.4 percent pursue social/recreational activities alone, 28.9 percent pursue only “go out/hang out”, 8.1 percent pursue only visit public place, 49.1 percent pursue only visit friends/family, and 4.6 percent pursue two discretionary activity events (but with the same accompaniment type choice). No individual pursues more than two discretionary special events on the same weekend day in this data set. It is found that 34.1 percent of the activities are undertaken alone, 20.8 percent involve non-household members, and 45.1 percent involve exclusively household members. This suggests that a large proportion of weekend discretionary activities are pursued only with household members. The go out/hang out activity exhibits the longest average duration at about three hours, followed by social/recreational activity at about 2.5 hours. The shortest duration is exhibited by visit public place at just about 1.5 hours. The table also furnishes the number of observations that fall into different duration bands and the number of individuals pursuing the different discretionary activity event alternatives.

Overall, the data set is quite suitable for modeling weekend discretionary activity participation, time allocation, and accompaniment type. The socio-economic and demographic profile of the respondent sample does not present any unusual anomalies. In the interest of brevity, a detailed tabulation and description of the survey sample is not provided here. Suffice it to say that the sample was thoroughly checked to ensure that it was suitable for use in this study.

## **5. MODEL ESTIMATION RESULTS**

This section presents the model estimation results. Several categories of exogenous variables were considered in the model specification including (1) individual characteristics, (2) household characteristics, and (3) location attributes. Individual characteristics considered include gender, age, and employment status. The household characteristics considered were household size, presence and number of children, number of adults, household composition, residential tenure, and vehicle ownership. In terms of location attributes, residential location (categorized as urban and rural) was considered.

As discussed earlier, the choice context being examined consists of 46 alternatives. Estimating all potential exogenous variable effects for all of the alternatives would result in a cumbersome and likely inefficient model specification. Hence, in this paper, variable effects are considered across the event type and accompaniment type dimensions. This allows capturing a majority of the exogenous variable impacts while retaining a parsimonious specification. The overall variable specification process was also guided by behavioral intuitiveness and prior research.

### **5.1. Model Specification**

The empirical analysis involved estimating six different copula-based structures (Gaussian, FGM, Frank, Gumbel, Clayton, and Joe) as well as the independent structure. For asymmetric copulas the traditional Lee’s transform based dependency and the non-traditional dependency were also estimated. The Bayesian Information Criterion (BIC) test was employed to determine the preferred

model structure as the different model structures are not nested within one another. The BIC for a given empirical model is equal to  $-2\ln(L) + K \ln(Q)$ , where  $\ln(L)$  is the log-likelihood value at convergence,  $K$  is the number of parameters, and  $Q$  is the number of observations. The model with the *lower* BIC value is the preferred model. For the different copula models with the same number of parameters, the BIC effectively translates into a comparison of the log-likelihood. The Joe copula with the traditional dependency offered the superior fit among the various models considered. The log-likelihood value at convergence for the Joe copula-based model was found to be -3159.65. The likelihood value at convergence for the independent model structure was -3161.86. The BIC values for the Clayton copula-based model and the independent model were 6558.67 and 6563.09 respectively. Clearly, the BIC values confirm that the copula-based model offers statistically superior fit compared to the independent model. The log-likelihood and BIC values for the Gaussian copula were -3161.21 and 6561.79 respectively, clearly highlighting the increased flexibility offered by the copula approach. In addition to the Joe and Gaussian copulas, the Clayton and Gumbel copula model with traditional dependency also outperformed the independent model. In the interest of brevity, only a discussion of results for the Joe copula model is presented here.

## 5.2. Discrete Component

For the discrete component of the model (joint consideration of the type of discretionary activity pursued and the accompaniment type chosen), several GEV structures and the multinomial logit specifications were estimated. The GEV models were estimated with correlation across the accompaniment type dimension, i.e., alternatives of the same accompaniment type were postulated as exhibiting stronger substitution patterns within distinct activity types. Alternative model specifications were tested for nested dependencies across the discrete choice combination alternatives. After extensive testing, it was found that the GEV structures we tested were not supported in this empirical model estimation exercise; the model repeatedly collapsed to the standard multinomial logit specification. The remainder of the discussion in this paper is based on the multinomial logit model specification for the discrete component of the model.

Estimation results are furnished in Table 2 for the MNL discrete model component. Among individual attributes, it is found that males are less likely to pursue social/recreational activities. Teenagers in the age group of 14-19 years are more likely to pursue “go out/hang out”, a finding that is consistent with expectations. Among household demographics, several behaviorally intuitive findings can be discerned. Car ownership is positively associated with “go out/hang out”; on the other hand, the presence of children and the presence of multiple adults have a negative impact on the pursuit of “go out/hang out” activities. This finding is consistent with expectations in that individuals in families with children and multiple adults are less likely to “hang out”. On the other hand, individuals in households with multiple adults are more likely to visit a public place. The presence of children is positively associated with joint activity engagement, whether with household members alone or including non-household members as well, an indication that children spur joint activities in the family and beyond. Individuals who live in households that own their residence are likely to be in family households; as a consequence residential tenure (own) is positively associated with family member accompaniment choice. There is a weak, albeit positive relationship between number of workers in the household and pursuit of social/recreational activities. Single adults (with no children) are more likely to pursue discretionary activity events with non-household members (relative to the base alternative “alone”), a sign of the need for social contact. Couples and single parents are more likely to pursue

discretionary activity events on weekends with family members. Couples are also less likely to engage in go out/hang out as evidenced by the negative coefficient associated with the two adult-no children family composition in this activity type choice.

Household income has a positive, albeit statistically insignificant impact on go out/hang out. Income has a negative impact on visit friend/family activity type choice and on pursuing discretionary activity events with non-family members. It is likely that high income households are also multi-adult families with or without children. Individuals in such households are likely to pursue activities jointly with other household members as opposed to non-family members. It is found that individuals living in urban areatype are more likely to pursue social/recreational, go out/hang out, and visit friend/family activities. This is consistent with the notion that access to such activity destinations is likely to be superior in urban environments. Individuals residing in urban environments appear less inclined to pursue activities with family members, presumably because urban dwellers are young and single.

### **5.3. Continuous Duration Component**

Results of the continuous duration model component are presented in Table 3. The threshold parameters (for the group duration interval categories) do not have a behavioral interpretation, but simply serve as cutoff points to map the grouped intervals to the continuous underlying latent duration propensity measure which is unobserved. It should be noted that a single set of thresholds for all 15 discretionary event participation alternatives was estimated in this effort (instead of estimating  $15 \times 8 = 120$  parameters). This restriction provided an efficient and parsimonious model specification. However, to account for possible differences among the different combinations, deviations or shifts in thresholds were estimated for selected activity types and accompaniment type dimensions. These shift coefficients account for differences in thresholds across different alternative combinations.

The model estimation effort showed that the choice alternatives of “go out/hang out” and “visit friends/family” have thresholds that are different from the common set of thresholds presented in the top section of Table 3. These deviations are found to be positive and significant implying that alternative combinations that involve these activity type categories are likely to have longer durations than alternative combinations that do not involve these activity type alternatives.

An examination of the impact of exogenous variables suggests that those aged 26-40 years pursue discretionary activity events for shorter durations relative to other age groups. It is likely that this young-middle age group consists of busy individuals, possibly with young children in the household. As a result, their activity participation duration is shorter. Employed individuals (who presumably work primarily on weekdays) spend longer duration at discretionary activity events. Car ownership is positively associated with activity duration; with higher levels of car ownership, vehicle use constraints are eliminated. If there is no competition for the use of household vehicles, then individuals can afford to spend longer duration at activities. Household income has a negative impact on activity duration, possibly suggesting that higher income individuals pursue other types of activities (such as shopping and eat meal), thus leaving less time for discretionary activity duration.

### **5.4. Copula Parameter**

The copula parameter for the Joe-copula model with the traditional dependency structure highlights the presence of significant unobserved component that affects the discretionary activity event participation choice as well as the activity duration. The significant traditional dependency

parameter indicates that the correlation between the random error term in the discrete choice combination and the duration choice exhibits a negative relationship. In summary, the result clearly underscores the importance of accommodating unobserved heterogeneity in modeling the special event participation.

### **5.5. Elasticity Estimates**

Based on the model parameter estimates, it is possible to compute elasticities of activity engagement and time allocation. The elasticity values are furnished in Tables 4 and 5 for the entire survey sample. The elasticities are computed across the activity type dimensions rather than across all 46 alternatives in the choice set. Thus, elasticity estimates are generated for the five broad activity type choice categories.

The elasticity estimates in the MNL component (Table 4) reflect the percent change in the likelihood of pursuing an activity type for a unit (percent) change in the exogenous variable. It is found that social/recreation activity participation is highly influenced by urban residential location choice. Those living in urban areas are 61.8 percent more likely to pursue social/recreational activity, and about 40 percent more likely to pursue “go out/hang out” activity, than those not living in urban environments. Equivalently, those living in non-urban areas are much more unlikely than urban dwellers to participate in discretionary activity, which has important implications for social exclusion considerations (see next section). Similarly, those in the age group of 14-19 years old are much more likely to engage in go out/hang out in comparison to other age groups. On the other hand, males are much less likely to engage in social/recreational activities. A unit increase in the number of adults in the household greatly increases the propensity to visit a public place. Those residing in an urban environment are more likely to go out/hang out, and less likely to visit a public place. All of these findings are consistent with expectations.

Elasticity estimates in Table 5 pertain to those for the continuous duration component. A positive elasticity implies an increased likelihood of falling into a certain duration interval and a negative elasticity implies just the opposite. Consistent with model estimation results, it is found that those aged 26-40 years, in households with more adults, and in high income households are more likely to choose shorter durations. Those who are employed and reside in households with more vehicles are likely to allocate larger durations to their weekend discretionary activity episodes.

## **6. CONCLUSIONS**

Despite the growing recognition of the importance of weekend activity-travel demand, there have been a limited number of studies devoted to the study of such behavior. The current study augments existing literature on weekend activity-travel pattern analysis by examining individual participation and time allocation to discretionary activity events during the weekend days. Specifically, the current study develops a comprehensive framework to model (1) event type participation, (2) duration of participation and (3) accompaniment type (i.e., with whom the individual participates in the special event).

The study formulates a joint discrete-continuous framework for analyzing these dimensions. Specifically, the combination of event type and accompaniment type constitutes the discrete component while the duration of participation constitutes the continuous component. As a non-zero duration is observed for a particular discrete alternative only if a participation has occurred, it is critical to consider self-selection in the model structure. This is accomplished in this study using a copula-based sample selection approach that ties the discrete choice error component

with the duration error component in a flexible manner. The copula approach allows the testing of several flexible dependence structures rather than pre-imposing restrictive distributional assumptions.

An important observation from our results is that non-urban dwellers participate very little in social/recreational activity and in “go out/hang out” activity. That is, non-urban dwellers may be facing social exclusion issues (broadly defined as the “inability to participate fully in society”, one aspect of which is not being able to participate in the “normal activities of daily life”; see Farber (28)). This is a rather worrisome issue, because it is well established in the sociological literature that out-of-home discretionary and rejuvenating relaxation activities are important for human mental and physical well-being (see, for example, Voorpostel (29)). The implication is that there is a need to examine the reasons for this relative lack of participation in discretionary activities among non-urban dwellers, and address this situation. This is particularly important as the rural population in many areas of the United States is increasing, as the so-called baby-boomers look for retirement places and appear to be transplanting themselves in rural areas in the south, especially at the fringes of metropolitan areas (see LaMondia and Bhat (30)). The result is that not only is the population of rural areas in some parts of the US increasing, but it is also getting increasingly gentrified with retired people. Such individuals, in general, are time-rich but also physically less mobile than their younger peers, which underscores the need to design socially inclusive communities in non-urban areas.

The primary source of the data used in the paper is the 2008-2009 National Household Travel Survey for the Greater Phoenix metropolitan region in Arizona, comprising a sample of 1773 individuals who reported their activity-travel patterns for one weekend day. The empirical analysis involved estimating six different copula-based structures (Gaussian, FGM, Frank, Gumbel, Clayton, and Joe) as well as the independent structure with the traditional dependency structure (Lee’s form) and a non-traditional dependency structure. The Bayesian Information Criterion test is employed to determine the preferred model as the different model structures are not nested within one another.

The Joe copula model offered the superior fit among the various copula models considered. The model results clearly highlight the presence of significant self-selection effects of activity participation decisions on activity duration. A host of exogenous variables including individual characteristics, household characteristics, and location area type were considered in the model specification. The results highlight the significance of these variables in discretionary event participation, accompaniment type, and activity duration. The most significant variables influencing the choice of participation and duration include age and gender at the person level, and number of adults, vehicle ownership, presence of children, and family composition at the household level. The copula parameter is significant suggesting that the prediction of activity durations will be adversely affected if the potential endogeneity across the discrete choice participation alternative and the duration are neglected. Further, the results also highlight the flexibility of the copula approach in capturing various forms of dependencies in the decision process.

To be sure, the study is not without limitations. Specifically, the analysis would significantly benefit from considering social network characteristics in modeling discretionary special event participation. Additionally, future work in this domain should explore the use of more complex generalized extreme value structures for representing the dependencies across the discrete and continuous choice dimensions. Data collection efforts accurately defining

discretionary special events will also be critical to enhancing the modeling of such decision processes.

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**TABLE 1 Descriptive Analysis of Weekend Discretionary Activity Participation**

| <b>Special Event Activity Participation Rate and Average Duration (minutes)</b> |                      |                      |                               |                                   |
|---|----------------------|----------------------|-------------------------------|-----------------------------------|
| <b>Special Event Type</b>   | <b>Accompaniment</b> |                      |                               |                                   |
|   | <b>Alone</b>         | <b>With family</b>   | <b>With non-family</b>        | <b>Across Accompaniment Type</b>  |
|   | Avg. Duration (%)    | Avg. Duration (%)    | Avg. Duration (%)             | Avg. Duration (%)                 |
| Social / recreational   | 160.85<br>(4.2%)     | 150.22<br>(3.7%)     | 130.71<br>(1.5%)              | 151.91<br>(9.4%)                  |
| Go out / hang out   | 189.61<br>(7.9%)     | 181.89<br>(13.1%)    | 171.24<br>(7.9%)              | 181.09<br>(28.9%)                 |
| Visit public place  | 102.00<br>(1.5%)     | 76.75<br>(5.0%)      | 115.00<br>(1.7%)              | 89.13<br>(8.1%)                   |
| Visit friends / families  | 147.89<br>(18.5%)    | 123.93<br>(22.2%)    | 159.23<br>(8.3%)              | 138.95<br>(49.1%)                 |
| Aggregation of multiple special events  | 212.50<br>(2.1%)     | 264.60<br>(1.0%)     | 297.00<br>(1.5%)              | 251.23<br>(4.6%)                  |
| Across Event Type   | 161.12<br>(34.1%)    | 140.96<br>(45.1%)    | 167.90<br>(20.8%)             | 153.43<br>(100.0%)                |
| <b>Discrete Choice Component</b>  |                      |                      |                               |                                   |
| <b>Attributes</b>   |                      | <b>Accompaniment</b> |                               |                                   |
|   |                      | <b>Alone</b>         | <b>With household members</b> | <b>With non-household members</b> |
| Sample Size   |                      | 1773                 |                               |                                   |
| No Special Event  |                      | 1292                 |                               |                                   |
| Special Events<br>(Frequency)   | Social/recreational  | 26                   | 20                            | 9                                 |
|   | Go out/hang out      | 44                   | 66                            | 40                                |
|   | Visit Public Place   | 8                    | 26                            | 12                                |
|   | Visit Friend/family  | 96                   | 110                           | 46                                |
| <b>Duration Component</b>   |                      |                      |                               |                                   |
| Sample Size   |                      | 481                  |                               |                                   |
| Duration Categories<br>(Frequency)  | ≤30 minutes          | 70                   |                               |                                   |
|   | ≤60 minutes          | 45                   |                               |                                   |
|   | ≤90 minutes          | 54                   |                               |                                   |
|   | ≤120 minutes         | 43                   |                               |                                   |
|   | ≤150 minutes         | 61                   |                               |                                   |
|   | ≤180 minutes         | 56                   |                               |                                   |
|   | ≤240 minutes         | 68                   |                               |                                   |
|   | ≤360 minutes         | 55                   |                               |                                   |
| >360 minutes  | 29                   |                      |                               |                                   |

**TABLE 2 Joe Copula Model Estimates: MNL Component of Activity Participation Choice**

| Variables                                | Special Event Type Dimension |        |                 |        |                    |        |                            |        | Company Type Dimension |        |                           |        |
|--|------------------------------|--------|-----------------|--------|--------------------|--------|----------------------------|--------|------------------------|--------|---------------------------|--------|
|  | Social/<br>recreational      |        | Go out/hang out |        | Visit Public Place |        | Visit<br>Friend<br>/family |        | With Family<br>Member  |        | With non-family<br>member |        |
|  | Coef                         | t-stat | Coef            | t-stat | Coeff.             | t-stat | Coef                       | t-stat | Coef                   | t-stat | Coef                      | t-stat |
| <b><u>Individual Characteristics</u></b> |                              |        |                 |        |                    |        |                            |        |                        |        |                           |        |
| Gender                                   |                              |        |                 |        |                    |        |                            |        |                        |        |                           |        |
| Male                                     | -0.832                       | -2.590 | -               | -      | -                  | -      | -                          | -      | -                      | -      | -                         | -      |
| Age                                      |                              |        |                 |        |                    |        |                            |        |                        |        |                           |        |
| 14-19                                    | -                            | -      | 0.999           | 2.875  | -                  | -      | -                          | -      | -                      | -      | -                         | -      |
| <b><u>Household Demographics</u></b>     |                              |        |                 |        |                    |        |                            |        |                        |        |                           |        |
| Number of Cars                           | -                            | -      | 0.214           | 2.065  | -                  | -      | -                          | -      | -                      | -      | -                         | -      |
| Number of Children                       | -                            | -      | -0.163          | -1.663 | -                  | -      | -                          | -      | 0.178                  | 2.043  | 0.370                     | 4.870  |
| Number of Adults                         | -                            | -      | -0.274          | -1.951 | 0.774              | 2.699  | -                          | -      | -                      | -      | -                         | -      |
| Residential Tenure                       |                              |        |                 |        |                    |        |                            |        |                        |        |                           |        |
| Own residence                            | -                            | -      | -               | -      | -                  | -      | -                          | -      | 0.696                  | 1.885  | -                         | -      |
| Number of worker                         | 0.177                        | 1.318  | -               | -      | -                  | -      | -                          | -      | -0.379                 | -3.357 | -                         | -      |
| Family composition                       |                              |        |                 |        |                    |        |                            |        |                        |        |                           |        |
| One adult and no children                | -                            | -      | -               | -      | -                  | -      | -                          | -      | -                      | -      | 0.738                     | 2.019  |
| Two adult and no children                | -                            | -      | -0.439          | -1.635 | -                  | -      | -                          | -      | 0.487                  | 2.094  | -                         | -      |
| Single parent                            | -                            | -      | -               | -      | -                  | -      | -                          | -      | 0.901                  | 1.788  | -                         | -      |
| Number of drivers                        | -                            | -      | -               | -      | -0.635             | -1.693 | -                          | -      | 0.274                  | 1.859  | -                         | -      |
| Household income                         | -                            | -      | 0.017           | 1.100  | -                  | -      | -0.016                     | -1.551 | -                      | -      | -0.024                    | -1.530 |
| <b><u>Location Attributes</u></b>        |                              |        |                 |        |                    |        |                            |        |                        |        |                           |        |
| Urban                                    | 1.179                        | 2.215  | 0.852           | 2.518  | -                  | -      | 0.538                      | 2.035  | -0.625                 | -2.173 | -                         | -      |

**TABLE 3 Joe Copula Model Estimates: Activity Duration Component**

| <b>Variables</b>                             | <b>Coefficient</b> | <b>t-stat</b> |
|--|--------------------|---------------|
| <b><u>Threshold parameters</u></b>           |                    |               |
| 30 minutes                                   | -1.760             | -7.188        |
| 60 minutes                                   | -1.005             | -4.318        |
| 90 minutes                                   | -0.546             | -2.381        |
| 120 minutes                                  | -0.166             | -0.727        |
| 150 minutes                                  | 0.201              | 0.865         |
| 180 minutes                                  | 0.576              | 2.420         |
| 240 minutes                                  | 1.114              | 4.658         |
| 360 minutes                                  | 1.707              | 7.731         |
| <b><u>Threshold Shifts</u></b>               |                    |               |
| Event type dimension                         |                    |               |
| Go out/hang out                              | 0.856              | 4.811         |
| Visit Friend/family                          | 0.444              | 3.189         |
| <b><u>Individual Characteristics</u></b>     |                    |               |
| Age  |                    |               |
| 26 – 40                                      | -0.351             | -2.003        |
| Employment status                            |                    |               |
| Employed                                     | 0.187              | 1.676         |
| <b><u>Household Demographics</u></b>         |                    |               |
| Number of cars                               | 0.159              | 2.449         |
| Number of adults                             | -0.129             | -1.572        |
| Household income                             | -0.035             | -3.936        |
| Copula Parameter (same for all alternatives) | 1.059              | 40.653        |

**TABLE 4 Elasticity Estimates: MNL Activity Type Choice Component**

| <b>Variables</b>                         | <b>No special event</b> | <b>Social/recreational</b> | <b>Go out/hang out</b> | <b>Visit Public Place</b> | <b>Visit Friends/family</b> |
|--|-------------------------|----------------------------|------------------------|---------------------------|-----------------------------|
| <b><u>Individual Characteristics</u></b> |                         |                            |                        |                           |                             |
| Gender                                   |                         |                            |                        |                           |                             |
| Male                                     | 2.309                   | -74.463                    | 1.384                  | 1.346                     | 1.412                       |
| Age                                      |                         |                            |                        |                           |                             |
| 14-19                                    | -11.966                 | -7.058                     | 128.656                | -6.631                    | -7.076                      |
| <b><u>Household Demographics</u></b>     |                         |                            |                        |                           |                             |
| Number of Cars                           | -1.947                  | -1.162                     | 20.950                 | -1.074                    | -1.158                      |
| Number of Children                       | -3.212                  | 13.223                     | -3.238                 | 13.326                    | 13.344                      |
| Number of Adults                         | -0.972                  | -0.515                     | -23.345                | 111.099                   | -0.626                      |
| Residential Tenure                       |                         |                            |                        |                           |                             |
| Own residence                            | -6.732                  | 17.287                     | 17.725                 | 18.526                    | 18.097                      |
| Number of worker                         | 3.445                   | 6.472                      | -10.794                | -11.160                   | -10.940                     |
| Family composition                       |                         |                            |                        |                           |                             |
| One adult and no children                | -5.332                  | 14.676                     | 13.820                 | 14.362                    | 14.361                      |
| Two adult and no children                | -3.053                  | 19.330                     | -21.568                | 20.340                    | 20.203                      |
| Single parent                            | -14.733                 | 37.918                     | 38.930                 | 40.539                    | 39.508                      |
| Number of driver                         | 6.160                   | -14.366                    | -14.778                | -35.405                   | -14.596                     |
| Household income                         | 0.207                   | -0.318                     | 1.291                  | -0.298                    | -1.749                      |
| <b><u>Location Attributes</u></b>        |                         |                            |                        |                           |                             |
| Urban                                    | -8.245                  | 61.807                     | 40.840                 | -36.951                   | 16.193                      |

**TABLE 5 Elasticity Estimates: Activity Duration Component**

| Variables                                | Duration   |            |            |             |             |             |             |             |              |
|--|------------|------------|------------|-------------|-------------|-------------|-------------|-------------|--------------|
|  | 30 minutes | 60 minutes | 90 minutes | 120 minutes | 150 minutes | 180 minutes | 240 minutes | 360 minutes | >360 minutes |
| <b><u>Individual Characteristics</u></b> |            |            |            |             |             |             |             |             |              |
| Age                                      |            |            |            |             |             |             |             |             |              |
| 26 – 40                                  | 32.364     | 20.757     | 12.568     | 6.068       | 0.142       | -5.529      | -11.754     | -18.059     | -25.890      |
| Employment status                        |            |            |            |             |             |             |             |             |              |
| Employed                                 | -15.779    | -10.889    | -7.210     | -4.113      | -1.125      | 1.910       | 5.485       | 9.408       | 14.890       |
| <b><u>Household Demographics</u></b>     |            |            |            |             |             |             |             |             |              |
| Number of cars                           | -12.696    | -9.206     | -6.418     | -3.966      | -1.509      | 1.078       | 4.252       | 7.892       | 13.308       |
| Number of adults                         | 11.368     | 7.552      | 4.789      | 2.535       | 0.421       | -1.665      | -4.042      | -6.556      | -9.882       |
| Household income                         | 2.959      | 2.027      | 1.329      | 0.745       | 0.185       | -0.380      | -1.039      | -1.753      | -2.735       |