

Final Report–Visualizing the Output Data of SUNTANS using ArcGIS

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Abstract

This report discusses a method of using ArcGIS to visualize the results of a numerical model SUNTANS. ArcGIS is a powerful tool of visualizing and analyzing data. For both large and small study domain, it is able to present persuasive figures. By adding different layers, such as fresh water source and NHDPlus, the key features of results of a numerical model can be well presented. Meanwhile, the correctness of the model bathymetry and boundary conditions can be checked by comparing with the existing dataset. In the report, different model outputs, such as velocity, free surface elevation, temperature and salinity, are visualized. By analyzing the distribution and time variation of salinity, the conclusion that river discharge and tidal effect play a significant role in salt structure of San Francisco Bay is obtained. The results also suggest a comprehensive consideration of freshwater source. And a long-period run is needed to study the tidal effects.

Keywords: ArcGIS, SUNTANS

1 Introduction

San Francisco Bay is located in the state of California, surrounded by a contiguous region, covering somewhere between 400 and 1600 miles. Several estuaries in this Bay system serve as observational examples in the study of salt balance in estuaries. San Francisco Bay is also a mecca for sailors due to its strong wind system. The variability of San Francisco Bay is characterized by many mechanisms, such as tidal effects, freshwater discharge and exchange flow [1]. Therefore, it is valuable to study the hydrodynamic properties in this Bay system.

A three dimensional unstructured non-hydrostatic numerical model, SUNTANS (Fringer et al. [2]), is used to implement this study. This model allows a complete solution of the governing equation and solves on triangular mesh. Stacey et al. [3] tested the application of SUNTANS to San Francisco Bay and focused on South Bay. Both 2D and 3D validation of the model is provided. Chua et al. [4] did a similar study but focused on the northern reach. The northern San Francisco Bay is a partially-stratified estuary dominated by

17 seasonal-varying freshwater discharge, while the south bay is mainly affected
18 by tidal oscillation [4]. The visualization of SUNTANS has been implemented
19 in the platform of MATLAB and python, which gives a conceptual under-
20 standing of the data. Geographic Information System (GIS) is considered
21 as a powerful tool in presenting and processing data, and is thus capable of
22 visualizing the data of various flow and climate properties of San Francisco
23 Bay.

24 Before running a numerical model, GIS serves as a tool to check the input
25 grid and bathymetry files. Its efficiency of loading and presenting data from
26 various sources gives a clear view of the model frame and avoid primary mis-
27 takes, which may cause serious problems. In this report, to analyze the ability
28 that GIS helps complete an analysis of numerical model, I start with its func-
29 tion of presenting existing data from various sources. Then, the visualization
30 of the output data and related analysis is discussed. The advantage of GIS in
31 visualizing SUNTANS is taken into account in the end.

32 **2 San Francisco Bay and Model Setup**

33 In this section, a more detailed introduction of San Francisco Bay system is
34 presented including the characteristics of each composition. The model setup,
35 which are the boundary and initial conditions are discussed.

36 In figure 1, a plot indicating different systems that comprise the whole
37 San Francisco Bay area is presented. It is seen that there are basically five
38 components, which are Pacific Ocean, Suisun Bay, San Pablo Bay, Central
39 Bay and South Bay. The last two can also be combined and are called San
40 Francisco Bay. There are mainly two rivers flowing into Suisun Bay, which
41 are Sacramento and San Joaquin rivers, serving as large freshwater discharge.
42 Napa River flows into San Pablo Bay at the entrance. The whole bay area
43 is dominated by three large cities, San Francisco, Oakland, and San Jose.
44 And the famous Golden Gate is the North American strait that connects San
45 Francisco Bay to the Pacific Ocean.

46 Since the San Francisco Bay case of SUNTANS is only a test case intro-
47 duced by its developers to test the model practicability, the boundary and
48 initial conditions are assumed to be simple. For the boundary condition, there
49 are three kinds of edges, which are closed boundaries, open or velocities spec-
50 ified boundaries and open or stage-specified boundaries. Since the values at
51 the closed boundaries are considered zero, I only consider the boundary con-
52 dition at the river mouth and coastal area. The background temperature is
53 considered 0 in this study. QGIS, which is an open source software, is used to
54 generate a shape file to specify the edge ID for the velocities specified bound-
55 ary. The Sacramento river and San Joaquin river serve as two river discharge
56 at this boundary. However, the river fluxes at these sites are set to be zero
57 by the developers, which may distort the truth in estuary dynamics. Since
58 we focus on the way that ArcGIS visualize the output data in this report,

59 the introduction of model setup only assists to understand the results. In the
 60 stage-specified boundary, the background salinity is assumed to be 32 psu for
 61 the sea water. The harmonic analysis of tide is used to represent the tidal
 62 effects, where the oscillatory water level can be indicated as follows,

$$h = h_0 + hamp \times \cos(\omega t) \quad (1)$$

63 where h is the surface elevation at the boundary. $h_0 = -5m$ is free surface at
 64 the initial condition. $\omega = \frac{2\pi}{12.42 \times 3600}$ is the tidal frequency. $hamp = 0.5$ is the
 65 tidal range. For the initial condition, the temperature and salinity are assumed
 66 to change linearly as the location approaches inland with the background value
 67 of 0 and 32 psu, respectively. The wind condition is also added to the model
 68 but details will not be discussed here. Baston and Harris [5] did a similar
 69 study with more realistic boundary and initial conditions in Pentland Firth
 70 and studied the effect of tidal flow.

71 With the information of San Francisco Bay and SUNTANS model setup,
 72 it is ready to analyze the model output data with the help of ArcGIS.

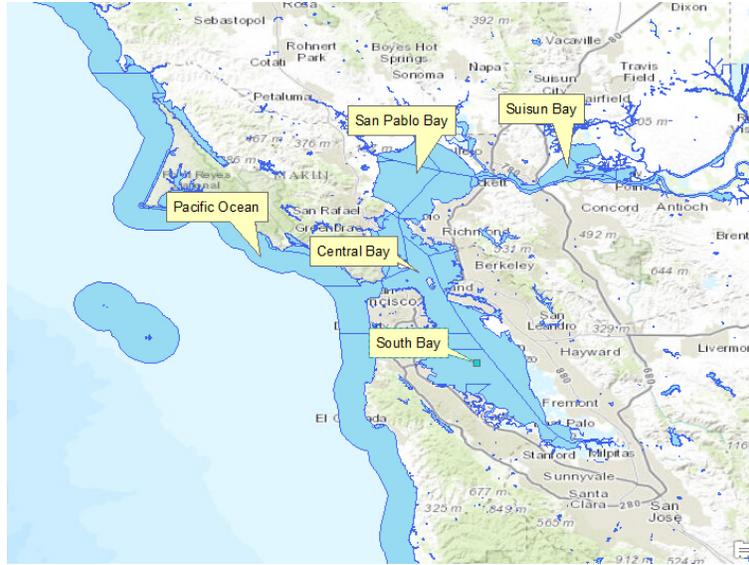


Figure 1: Detailed Composition of San Francisco Bay

73 3 Visualization of Model Grid and Bathymetry

74 In this section, the ability of ArcGIS in checking the model input data is
 75 discussed. Before a normal run, it is always thoughtful to check the input
 76 file in a different method to avoid basic mistakes. For example, the input
 77 bathymetry may be created using a certain script. Its correctness should not
 78 be taken as granted without comparing with the real topography. This process
 79 can be fulfilled by ArcGIS within seconds due to its large data source. The

80 ability of presenting the grid is also valuable. Since the grid file of some of the
81 numerical models is created by developers, the executors may lack the access
82 to visualize the grid, which can be compensated by the efficiency of loading
83 data in ArcGIS.

84 In this project, a two-dimensional run of the SUNTANS model in San
85 Francisco Bay is accomplished. Since the data format is NetCDF, a matlab
86 function is developed to decompose the data and transfer the original format
87 to that of excel, which can be read by ArcGIS.

88 The data projection datum used by SUNTANS is "NAD_1983_UTM_Zone_
89 10N" , and the earth datum is "D_North_American_1983". SUNTANS is a
90 triangle unstructured model, comprised of Delaunay triangle grid, with De-
91 launay points at the indices of each triangle and Voronoi points at the nearly
92 centered points. The grids are divided into three files, which are points, edges
93 and cells. Since these files are generated using a specific tool related with
94 SUNTANS, and the direct connections between cells and edges are the indices
95 of Delaunay points, I will not visualize the triangle grid in ArcGIS. Instead,
96 the Voronoi points of the San Francisco Bay, which represent the computing
points of water properties at each grid are visualized in figure 2. This figure

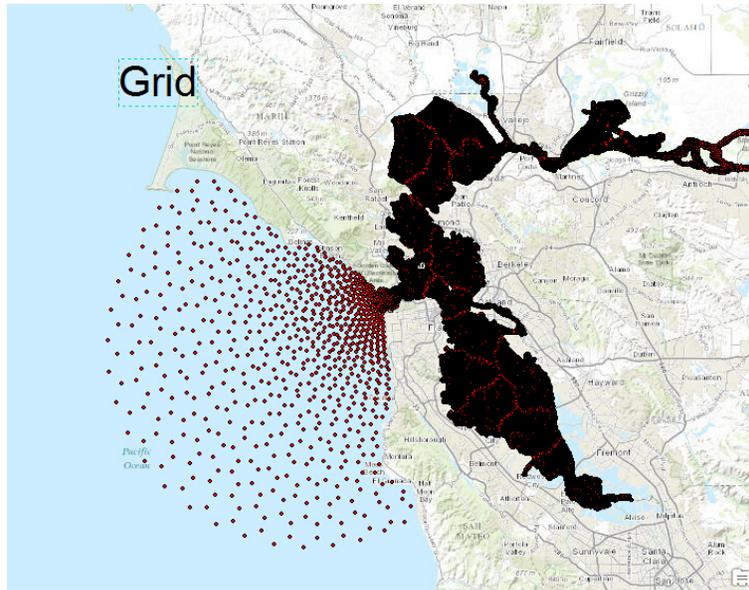


Figure 2: Model grid

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98 gives an overall view of the study area at the scale of full domain. It is seen
99 that the grids have a much lower resolution in the far coastal area than inside
100 the bay.

101 Once the grid is generated, the next requirement is to specify the depth
102 at each grid point. As illustrated by Stacey et al. [3], the bathymetry data
103 is collected from several different sources, including USGS soundings (2005),
104 USGS lidar (2005) and USGS coarse grid (ca 1995). The depth is stored in
105 a file called depth.dat. In SUNTANS, the developers use the interpolation

106 method of inverse distance weighting to attain the bathymetry file. However,
107 after comparing every spatial interpolation method in ArcGIS, the Natural
108 Neighbor method that can fit the bathymetry best is chosen. The defect of
109 this method is that it has included the values in the land. This happens during
110 the interpolation process and is because the computational area is not a poly-
111 gon. However, the powerful ability of presenting data in ArcGIS can neglect
112 the unnecessary parts due to interpolation by adding additional layers. Here
113 in this analysis, a bathymetry layer (COMMISSION FOR ENVIRONMEN-
114 TAL COOPERATION) is added to the map representing the land parts. The
115 Suisun Bay, which is considered as fresh water, is replaced by adding a layer
116 representing rivers and lakes. This treatment helps analyze the effect of river
117 discharge on salinity distribution.



Figure 3: Model input bathymetry

118 In figure 3, the model input bathymetry plotted by ArcGIS is given. The
119 deeper blue indicates larger depth, while light blue denotes shallower area.
120 The depth tends to decrease as it approaches inland. The mouth of the es-
121 tuary and the ship channel inside the bay area have larger depth. Whether
122 or not this input bathymetry represents the real topography can be checked
123 via its comparison with the existing data. The existing bathymetry data is
124 collected from San Francisco Bay Area Regional Database (USGS). Here, only
125 the data inside the bay area is available. In figure 4, the bathymetry based
126 on the USGS data is presented. Slight difference occurs between model input
127 and downloaded bathymetry data but the model input file preserves the key

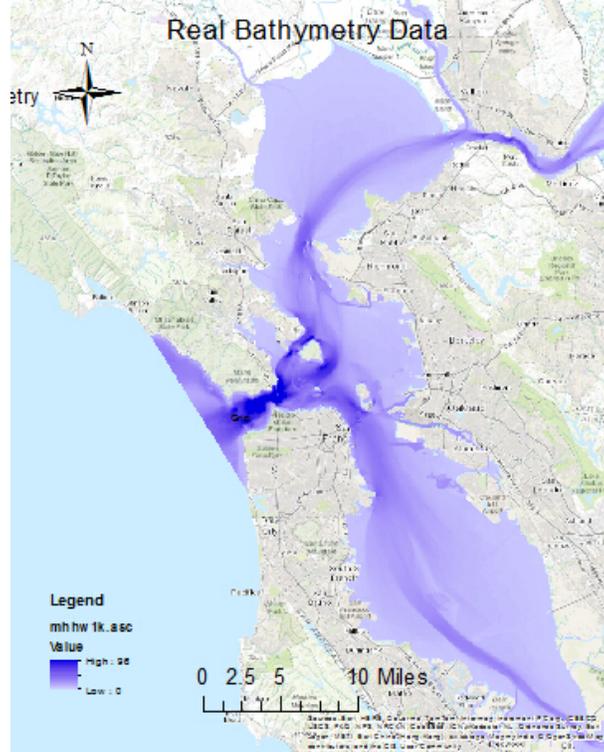


Figure 4: Real bathymetry data (USGS)

128 features of San Francisco Bay. Better results should be obtained if finer grid is
 129 used. The difference may result from interpolation method. In figure 3, since
 130 two methods (idw and Natural Neighbor) are used to interpolate the depth,
 131 the discontinuity may occur. Since the Natural Neighbor method presents a
 132 better result in ArcGIS, this method may be used to create the bathymetry
 133 file in the future.

134 In this section, ArcGIS plays an important role of presenting the grid file,
 135 providing a simple and direct way of viewing the resolution of the grid. In
 136 the comparison between the two bathymetry datasets, the data from USGS is
 137 used, which validates the model input bathymetry.

138 4 Visualization of the Output Data

139 In this section, several model output files are visualized using ArcGIS. By
 140 adding different datasets to the map, it becomes more convenient to capture
 141 the key features of the output data. Lakes and Rivers data collected from
 142 USGS and NHDPlus stream data are created as two different layers and are
 143 put on the top of the output data layer. This treatment provides a direct look
 144 into the fresh water discharge, which can affect the distribution of salinity.
 145 Note that the velocity, free surface elevation and temperature are the results
 146 of the last time step. The salinity data is presented at both the initial state

147 and the steady state.

148 In figure 5, the model output velocity profile is presented. Yellow denotes
149 negative values of approximately $-1.12 \text{ m/s} \sim -0.08 \text{ m/s}$. These negative
150 values indicate fresh water going into the sea. Ching represents small values
151 that fall between $-0.08 \text{ m/s} \sim -0.33 \text{ m/s}$. It is seen that Ching occupies
152 a large percentage in San Pablo Bay and South Bay. These values can be
153 considered as fluctuations and may result from the mixing between fresh water
154 and salty water. Deep blue denotes larger positive velocities ($0.43 \text{ m/s} \sim 0.85$
155), which is saltier sea water coming into the bay. Note that a small percentage
156 of deep blue occurs at the mouth of Suisun Bay, which is due to the suddenly
157 decreased channel width. This example case is a two-dimensional run, the
158 velocity values are considered at the water surface. In the classical estuarine
159 analysis, exchange flow occurs at the mouth of the estuary with fresh water
160 going out at the shallower part of the water column and sea water coming in
161 at the deeper part. The dominating negative values of velocity at the mouth
162 proves this theory. However, unexpected values exist in South Bay. A small
163 percentage of negative velocities are close to the mouth of San Lorenzo Creek
164 in South Bay, while the rivers with much larger fresh water discharges in San
165 Pablo Bay don't have similar features. This phenomenon needs a further study
166 in a smaller scale as was done by M. Stacy (2012), who used the same model
167 but focus on the South Bay alone.

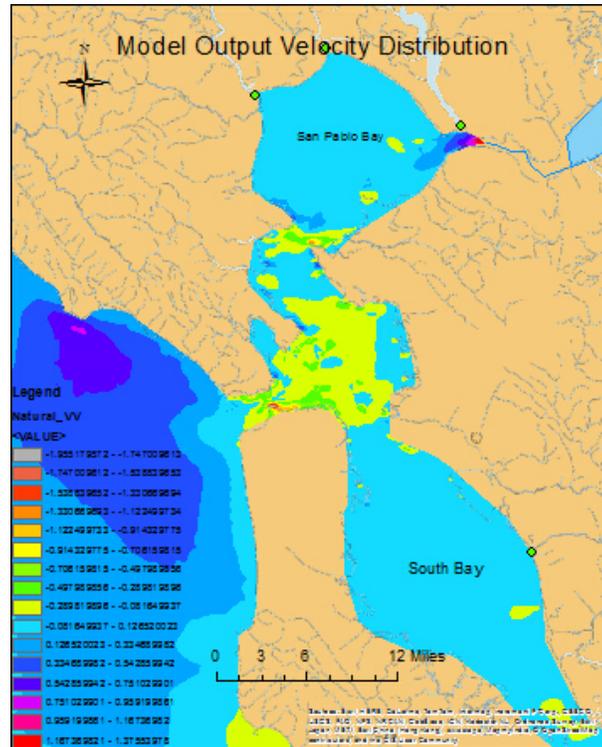


Figure 5: Model output velocity

168 In figure 6, the model output free surface elevation is shown. Dark green

169 that occupies San Pablo Bay and South Bay indicates small surface elevation
 170 with values approximate to $4.23\text{ cm} \sim 5.34\text{ cm}$. The warm color, yellow and
 171 red, denote larger values of $5.65\text{ cm} \sim 7.74\text{ cm}$. The largest free surface el-
 172 evation is at the mouth of San Francisco Bay, which results from the narrow
 173 channel at the mouth. And it is seen that as sea water is shoaling, the eleva-
 174 tion is gradually increasing. However the large river discharge of Napa River,
 175 Sonoma Creek and Petaluma River in San Pablo Bay don't seem to play an
 176 important role in the distribution of surface elevation. Since no large scale data
 177 is available in San Francisco Bay, proper observational sites near the mouth of
 178 these rivers should be chosen. And the time series of the observational data
 179 should be utilized to compare with the model result.

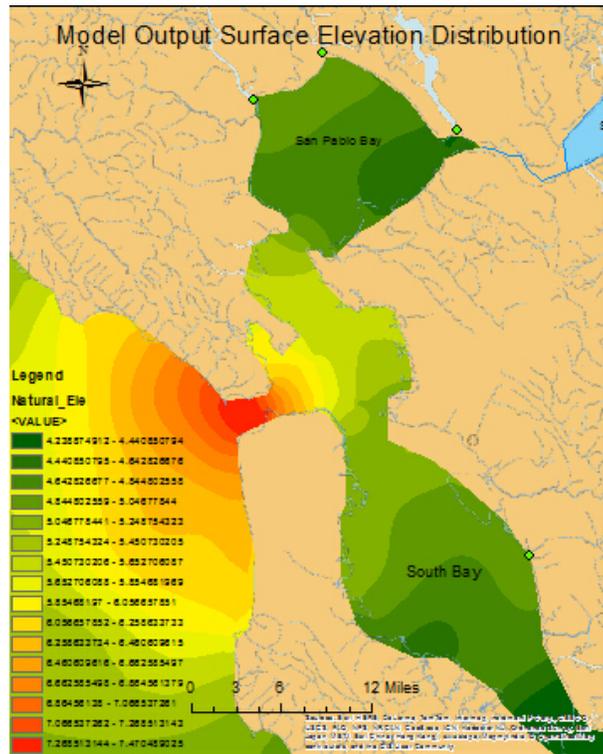


Figure 6: Model output free surface elevation

180 In figure 7, the SUNTANS output salinity distribution at the initial state
 181 is presented. The values of salinity fall between $0 \sim 32\text{psu}$ and 0 indicates
 182 fresh water. In this figure, yellow represents fresher water with small values,
 183 while red is saltier water with high values. However, as it is shown, salty water
 184 with high salinity occupies most part of San Francisco Bay, and only a small
 185 amount of fresh water occurs at the mouth of Suisun Bay. This figure, however,
 186 is not able to present the features in Suisun Bay, as it has been considered as
 187 a fresh water resource in the upper layer. In the model setup, two rivers (
 188 Sacramento River and San Joaquin River), which are inside Suisun Bay are
 189 considered. The initial salinity values at the mouth of these river (type 2
 190 boundary) are assumed to be zero. Although the result of Suisun Bay is not

191 shown in this report, the water in Suisun is occupied by fresh water with
 192 salinity values approximate to 0psu . Hence, the neglect of the effect of Suisun
 193 Bay is reasonable. The salty water dominated condition result from the initial
 194 background salinity, which is set to be 32psu .

195 Figure 8 presents the model output salinity of a more steady state, which
 196 is 24 hours later. The green bracket indicates a fresh water discharge and a
 197 mixing between fresh water and salty water. More obvious result of the fresh
 198 water discharge may be obtained from longer period of model run. However,
 199 after comparing the results of 12 hours later and 24 hours later, no obvious
 200 difference is found, which indicates that the assumed initial background salin-
 201 ity is not set properly, and the fresh water is not able to make enough effect
 202 on the salinity distribution even in San Pablo Bay under this condition. This
 203 example case only considered two fresh water resources (the initial salinity is
 204 set to be 0 at the mouth of two river). And the river fluxes are set to be 0
 205 at the mouths, which is not able to provide enough force to drive fresh wa-
 206 ter towards the sea. With these limitations in mind, the effect of fresh water
 207 discharge may be weakened compared with real condition.

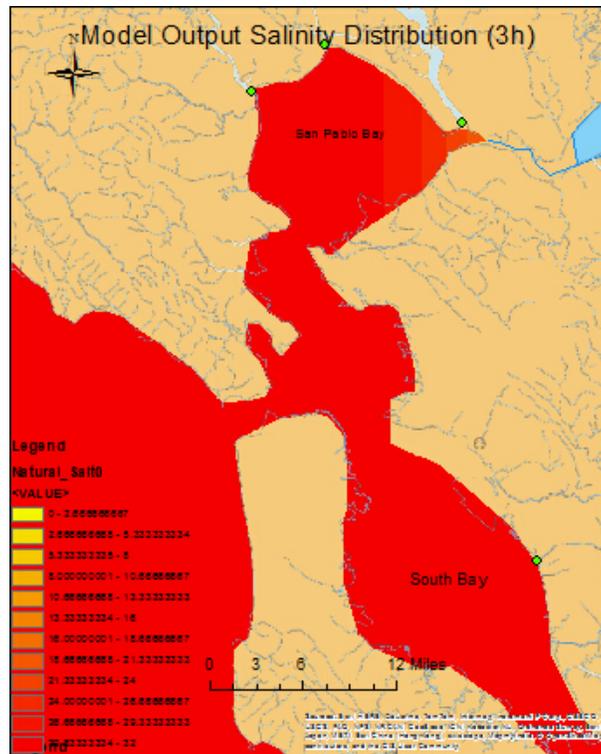


Figure 7: Model output salinity at initial state

208 The temperature distribution at the last time step is shown in figure 9. The
 209 result of temperature is consistent with that of salinity. In the figure, the white
 210 indicates the warmer sea water dominating in most parts of San Francisco Bay,
 211 while the pink in San Pablo Bay means cold fresh water brought by the river
 212 discharge.

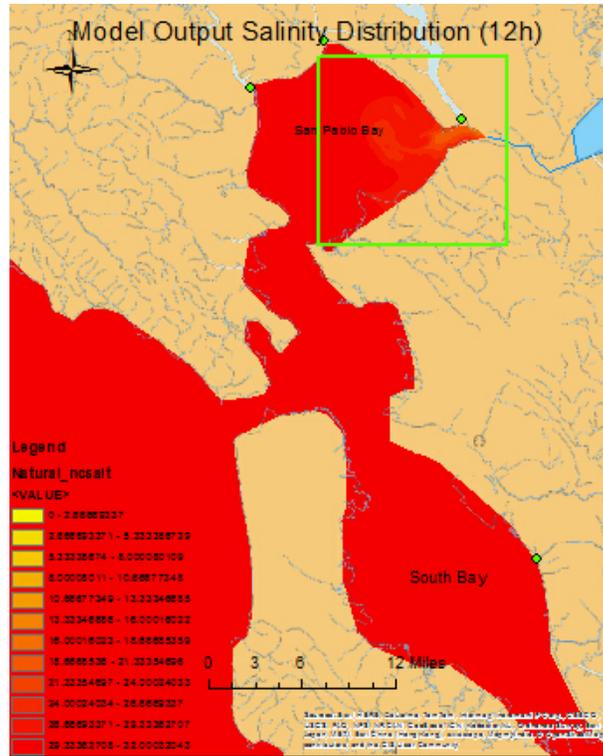


Figure 8: Model output salinity at steady state

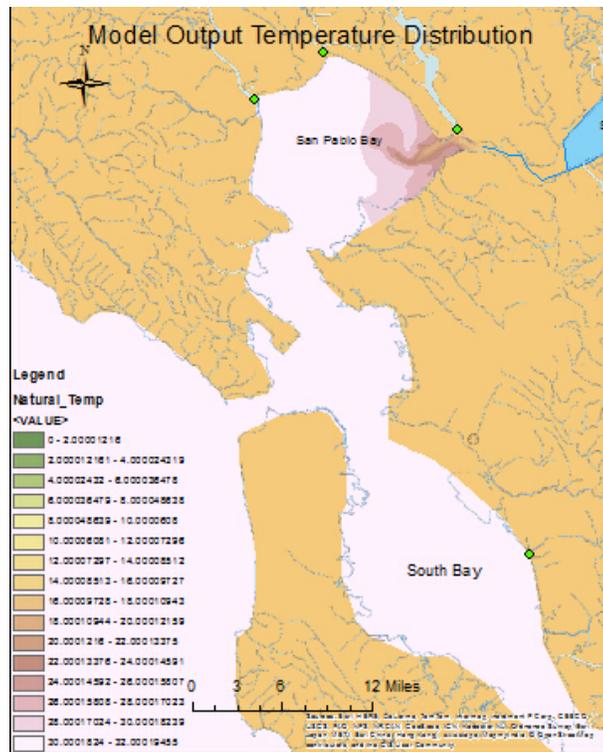


Figure 9: Model output temperature

213 **5 Discussion**

214 The data of salinity collected from USGS is presented in figure 10, where
215 darker yellow represents fresher water and lighter yellow denotes saltier water.
216 This salinity distribution is compatible with common sense. The water close
217 to the shore where river discharge exists is fresher, while saltier water intrudes
218 into the bay and dissipates. The distribution of observational data is different
219 with that of model output. Although the salinity distribution is related to
220 several effects in estuaries and varies with time. For example, there is obvious
221 difference of salinity distribution between flood and ebb, spring tide and neap
222 tide. The salinity data collected from USGS lack the time information and
223 the SUNTANS output data is based simply on the assumptions of the initial
224 condition. Depending upon this condition, it is reasonable to have different
225 distribution profiles.

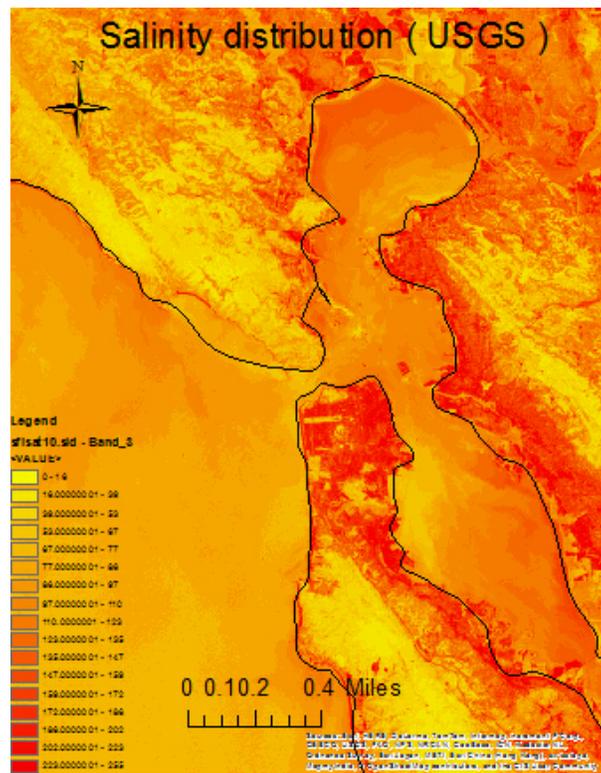


Figure 10: Salinity distribution (USGS data)

226 NHDPlus data provides an convenient method of pinpointing river mouth
227 and examining freshwater discharge of each river. It's important to check the
228 freshwater source before further discussion. In figure 11 and 12, the main
229 annual freshwater flows in San Pablo Bay and South Bay are presented. The
230 mean annual flows in Sacramento River and San Joaquin River are 24719.65
231 ft^3/s and 5966.199 ft^3/s , respectively. The effects of river discharge in Suisun
232 Bay is dominating compared with other effects, such as exchange flow, diffusive

233 flux and tidal effects. In San Pablo Bay, there are three main freshwater
 234 sources, which are Petaluma River, Sonoma Creek and Napa River. The mean
 235 annual flows are $133.762 \text{ ft}^3/\text{s}$, $172.6 \text{ ft}^3/\text{s}$ and $311.214 \text{ ft}^3/\text{s}$. Compared
 236 with those in Suisun Bay, the freshwater discharges in San Pablo Bay are
 237 small but may not be neglected to obtain reasonable results. In South Bay,
 238 no significant freshwater sources can be found in South Bay. The largest two
 239 indicated in figure 12 are San Lorenzo Creek and San Francisquito Creek with
 240 the annual mean flow of each being $21.676 \text{ ft}^3/\text{s}$ and $25.794 \text{ ft}^3/\text{s}$. No gaged
 241 watershed is considered. Therefore, the effects of river discharge should play a
 242 more important role in San Pablo Bay in the salinity distribution than South
 243 Bay. The neglect of these freshwater resources decrease the accuracy of the
 244 result. In the study of Stacey et al. [3], More freshwater sources, including
 245 major and minor rivers, small ungaged watersheds and wastewater returns
 246 are considered. And their running period is 15 days. Due to the limited
 247 computational resources and errors that come from MPI computing, I am not
 248 able to accomplish a multiple-processors run. So longer period is not tested in
 249 this review.

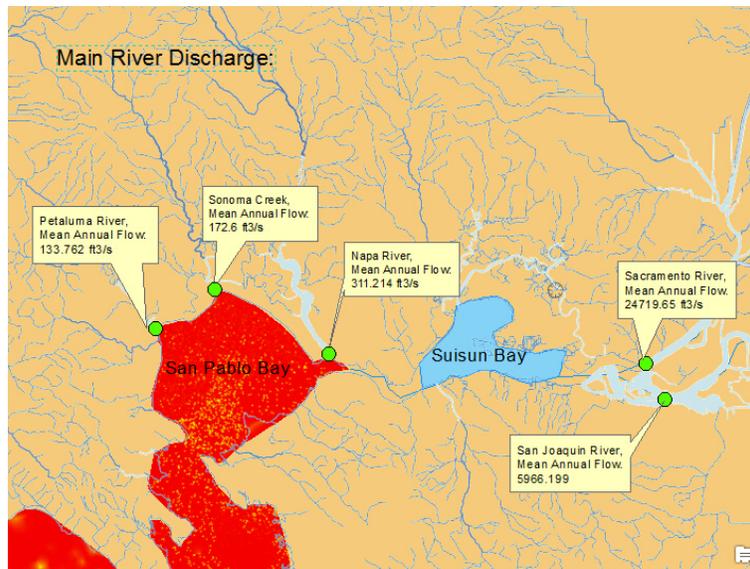


Figure 11: Freshwater source in San Pablo Bay

250 To compare the characteristics of salinity in San Pablo Bay and South Bay,
 251 several representative markers are chosen. By discussing the salinity variation
 252 with time at each marker, the effect of river discharge will be shown. In San
 253 Pablo Bay, I choose seven markers with the 1st starting at the mouth of Suisun
 254 Bay and the others extending towards the sea. The time variation of salinity
 255 at each marker is given in figure 13. As we can see, the variation of salinity
 256 near the mouth is more clear and becomes dumped towards the sea. At the
 257 1st marker, the variation has a range from 28 psu to 20 psu , while the range
 258 of variation of the four marker far from the mouth falls between 32 psu and
 259 30 psu . This figure is compatible with figure 8. As the effect of river discharge

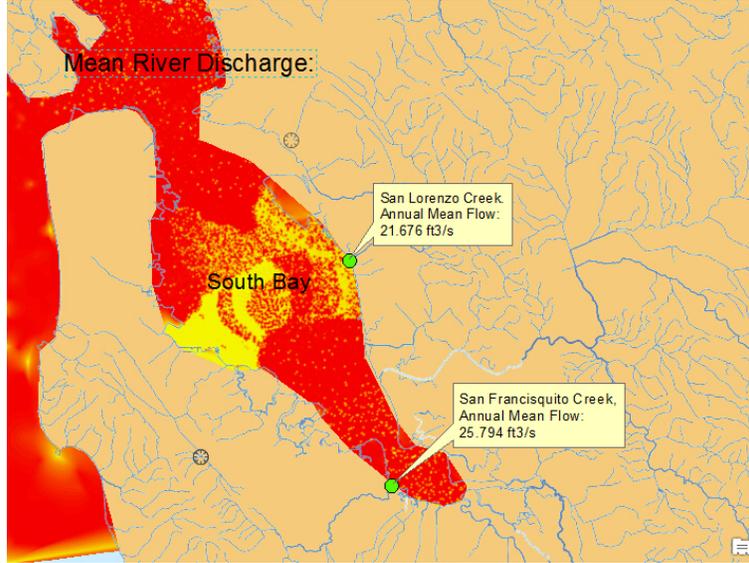


Figure 12: Freshwater source in South Bay

260 decreases, the time variation of salinity becomes small. As the marker is closer
 261 to the ocean, the salinity is close to the background salinity, which is 32 *psu*.
 262 Basically, the variation of salinity is periodic with the period of 12 hours. In the
 263 initial condition, the harmonic analysis rather than observational data is used
 264 to simulate the tide. The component of tide is semidiurnal component, M_2 that
 265 only considers the effect of earth rotation with respect to the Moon. The period
 266 of M_2 component is 12 hours, which is consistent with the period of salinity
 267 variation. This consistency indicates the tidal effects on the distribution of
 268 salinity. And this result agrees well with that of Stacey et al. [3]. In South
 269 Bay, I choose five marker starting from that close to the shore and extending
 270 towards the ocean. The time variation of salinity at these markers is shown
 271 in figure 14. There is only slight variation of salinity in South Bay. The
 272 range is between 31.999835 *psu* and 31.999810 *psu*. These variations may
 273 be neglected. The salinity is fluctuating over 24 hours and no trend can be
 274 found. No periodic variation indicates that tide is not affecting the salinity in
 275 South Bay strongly. This may be because the initial background salinity is not
 276 chosen properly. The South Bay is fulfilled with 32 *psu* salinity at the moment
 277 that the run starts. No freshwater source is another reason that no freshwater
 278 mechanisms exist in South Bay to adjust salinity. In the former study, tidal
 279 oscillation is dominating mechanism in the South Bay. However, the setup of
 280 unrealistic initial and boundary conditions, and the incomplete consideration
 281 of tide (M_2 tide only) make it difficult to conclude the tidal effect in South
 282 Bay.

283 By comparing the salinity distribution and time variation in San Pablo
 284 Bay and South Bay, we may have such conclusion that the river discharge
 285 play a significant role in salinity compared with other effects, which are wind,
 286 dispersion and exchange flow. Tidal effect is seen in San Pablo Bay but not

287 in South Bay. This may be because of the improper boundary and initial
 288 conditions. However, in order to obtain more accurate and persuasive re-
 289 sult, more freshwater sources should be added to the boundary conditions and
 290 longer run should be implemented. Plus, since this model run is a proof-of-
 291 concept exercise to establish the ability of ArcGIS to visualize the result of
 292 a numerical model. No specific sites are chosen and no related observational
 293 data is provided. There is no comparison between the time series of salinity
 294 and measurements. With this defect, it may be improper to assert that the
 295 model result is correct. (Chua et al. [4] tested the model performance in the
 296 northern reach and Stacey et al. [3] tested the model in South Bay under more
 297 realistic conditions). Further studies need to be done to validate the ability of
 298 SUNTANS to resolve dynamics in San Pablo Bay and even Central Bay.

299 In addition, the running period of SUNTANS in this project is not long
 300 enough to consider comprehensive effects made by tide. The period of 24
 301 hours is not able to present the salinity variation between flood and ebb tide,
 302 or spring and neap tide.

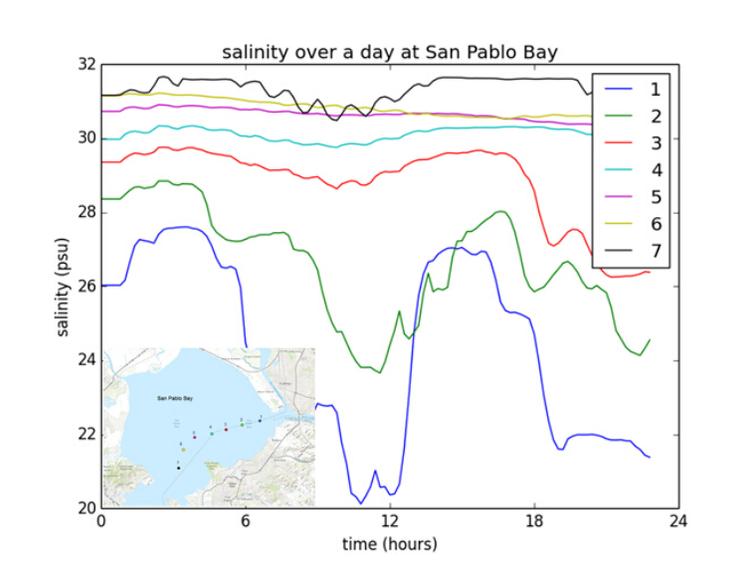


Figure 13: Freshwater source in San Pablo Bay

303 6 Summary

304 In this study, ArcGIS is proved to be a powerful tool in assisting the analy-
 305 sis of the result of a numerical model (SUNTANS). In the section of model
 306 setup, ArcGIS provides an efficient method of checking the model bathymetry
 307 and boundary conditions. By adding proper layers, such as NHDPlus, Lakes
 308 and Rivers (USGS), the freshwater sources can be found. In the section of
 309 visualizing the model output data, the interpolation tool, Natural Neighbor,
 310 is implemented, which results in the figures that can present different features

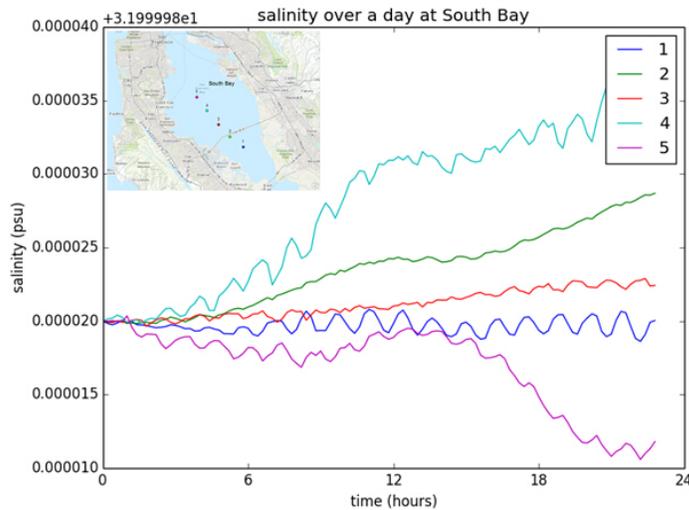


Figure 14: Freshwater source in South Bay

311 well. This well-performed interpolation method provides an alternative to the
 312 model developers in interpolating the depth. With the assistance of ArcGIS,
 313 the results in San Pablo Bay and South Bay indicate that river discharge plays
 314 an important role in salinity distribution and variation. The tidal effects that
 315 greatly affect the salinity variation in San Pablo Bay fail to make similar ef-
 316 fects in South Bay, which suggests that more freshwater sources should be
 317 considered and more realistic initial conditions (background salinity) should
 318 be applied.

319 In the further study, the same method (SUNTANS and ArcGIS) will be
 320 applied to my project, which is associated with Galveston Bay in Texas. The
 321 data of freshwater source and wind are more abundant and accessible in my
 322 research. The real-time tidal data can be obtained using the output of a
 323 Regional Ocean Model (ROMS) [6]. Hence, a more realistic study can be
 324 accomplished and animations should be made using ArcGIS as well.

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 328 the wonderful lectures throughout this semester. Thanks to Dr. Hodges and
 329 Dr. Rayson for the guide in running SUNTANS model.

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