ELECTRIC VEHICLE CHARGING STATION LOCATIONS:
RECOGNIZING ELASTIC DEMAND AND USER EQUILIBRIUM

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ABSTRACT
Battery-only electric vehicles (BEVs) generally offer better air quality through lowered emissions, along with energy savings and security. The issue of long-duration battery charging makes charging-station design and placement key for BEV adoption rates. This work uses genetic algorithms to identify profit-maximizing station placement and design details, with applications that reflect costs of installing, operating, and maintaining BEV service equipment, including land acquisition. BEV charging stations (EVCSs) are placed subject to stochastic demand for charging stations under a user-equilibrium traffic assignment. Random utility theory is used to determine BEV users’ station choices, considering endogenously determined (congested) travel times and on-site charging queues. The travel assignment with elastic demand problem is formulated as a convex program and is solved using a modified Frank-Wolfe algorithm.
Various realistic costs for power delivery and elastic demand patterns (to reflect driver sensitivities to travel times, wait times and charging costs) are used. Results for the Sioux Falls network suggest that EVCSs should locate mostly in the city center and along major highways. If a time horizon of just 3 years is used, and assuming that just 10% of BEV owners seek to charge en route each day, a user fee of $6 for a 30-minute charging session is not enough for station profitability (assuming land costs of $10,000 to $20,000 per year per station). However, a charging fee of $10 per BEV delivers a profit of about $130,000 per station, with just 1.3 cords per station on average in this coarse-network application. Based on sensitivity analysis, EVCS owner profits rise with a longer-term view (e.g., 5 to 10 years), shorter charging durations, more EVCS demand, and larger sites with more cords.

INTRODUCTION
Battery-only and plug-in electric vehicle (BEV and PEV) popularity is rising, thanks to environmental and energy benefits, falling battery and vehicle prices, and expanding consumer experience and education. PEVs generally offer better air quality through lowered emissions, along with energy savings and security, and lowered carbon footprints. PEVs are not only less expensive to operate and maintain than conventional (internal combustion engine) vehicles (Tuttle and Kockelman 2012; Simpson, 2006; Noori...
EV adoption and use rates are rising so fast chargers (DCFCs) in thousands of high-traffic commercial locations and along major freeways, many U.S., Chinese, European, and other travelers can now deliver significant charge to their PEVs in 30 min or less. For example, Tesla Model S users can add 170 miles to their batteries in 30 minutes at U.S. Tesla supercharging sites, and BMW i3 and Volkswagen e-Golf owners can charge deliver 60 to 80 miles in 30 minutes at similar sites (EVTown, 2015; Fleetcarma, 2018). As of August 2018, Tesla operates 10,738 superchargers in 1,333 stations worldwide, including 551 stations in the U.S., 53 in Canada, 11 in Mexico, 425 in Europe, and 293 in the Asia/Pacific region (Tesla, 2018). But queues are arising at many stations, while BEV and PEV adoption and use rates are rising (Voelcker, 2013). In addition, many travelers do not have decent access to charging stations at their homes (e.g., those in apartment buildings) or at their work places (EverCharge, 2017). Such travelers will not even purchase a PEV if they do not have good access. More stations are needed to support all these types of demand, and thereby encourage greater adoption and use of BEVs and PEVs. A salient question is where they should be placed.

LITERATURE REVIEW
Many economic decisions relate to location choices, of firms and firehouses, schools and transshipment warehouses. The goal is to serve demands efficiently while minimizing system costs or maximizing owner profits. Intensive studies of facility location started in the 17th Century when the Fermat-Weber Problem was introduced (Weber, 1909). Rather recently, researchers have investigated EVCS location choice.

Most EVCS research is based on optimizing facility location choice. The approaches used vary in terms of their objective functions, decision types, station types, application sizes, and candidate locations. Candidate locations are normally allowed to be a node in the network (He et al., 2018; Capar et al., 2013; Hanabusa and Horiguchi, 2011; Lee et al., 2014; Sageghi et al., 2014; Ghamami et al., 2016;) or special existing infrastructure, like parking lots and gas stations (Chen et al., 2013; Wang et al., 2010; Shahraki et al., 2015; Huang et al., 2016). Chen et al. (2013) formulated a mixed integer programming problem for optimal EV-charging-station location assignments across the Seattle region, minimizing PEV users’ station access costs while penalizing unmet demand. Current parking (and thus BEV-charging) demands were estimated via regression equations - as a function of zone accessibility, local jobs and population densities, trip attributes, and other variables available in most regions and travel surveys. When installing just 80 stations, their algorithms were able to serve 78% of parking demand within 1 mile of a CS cord, with a demand-weighted average access distance of 0.69 miles. He et al. (2018) coded a refueling-location model to identify optimal sites for EVCSs, to maximize the share of completed range-constrained long-distance highway travel across the U.S. (after clustering over 4000 National Use Microdata Area Zones into 196 trip-generation and –attraction points). They estimate that 93% and 99% of the nation’s long-distance ground-based passenger-vehicle trips can be completed with vehicle ranges of 200 and 300 miles, respectively, using just 100 EVCSs, thoughtfully located.

Some researchers do not use facility location optimization methods. For example, Shabbar et al. (2017) studied the estimated demand on a charging station by using a birth-and-death Markov-chain network model. They investigated the number of electric sockets needed, PEV waiting times, and average number of PEVs in queue at each station. Profit-maximizing CS locations, under both budget and routing constraints, were selected using a Grey Wolf Optimization algorithm. They conclude that commercial chargers should be used in early stages of infrastructure implementation, with superchargers enabling higher profits once the number of BEVs increases in the transportation network.

Some papers also consider queueing models, within their facility-location frameworks. However, they do not consider network congestion. Li and Su (2011) developed an optimal-cost model for EVCS with a minimum total-cost-of-service system, considering a queueing model at EVCS through waiting probability characteristics. Jung et al. (2014) proposed a bi-level simulation–optimization solution method.
to simulate a fleet of 600 shared-taxis in Seoul, Korea, considering itinerary-interception and queue delay.

Hess et al. (2012) presented a model for electric vehicles and their battery depletion, vehicle mobility, charging stations, and give a solution for the optimal placement of charging stations in a smart city. They considered queueing at EVCS and simulate electric vehicles through a genetic programming method.

One paper has investigated the EVCS location problem under network congestion. Lee et al. (2014) proposed a bi-level model to minimize the total failure cost under user equilibrium in route choice with a heuristic algorithm of simulated annealing. They applied their work using the Sioux Falls network, but did not consider queueing at stations or the number of chargers to be installed. Yao et al. (2014) developed a model, to minimize the overall annual cost of investment and energy losses while maximizing the annual traffic flow captured by fast charging stations through a user equilibrium-based traffic assignment model. However, it does not have congestion feedback on the station choices of the PEV users, and it does not consider queues at stations while just maximizing the flow at the station.

Overall, this work synthesis the facility location problem with network congestion and queueing at the charging stations, which is not often seen in current research. Further, this work is able to provide suggestion not only on station locations but detailed design in the stations in terms of the chargers so to minimize the cost over a time horizon while ensuring meeting the charging demand during a day. It provides an extension to most of current EVCS research in these aspects.

**METHODOLOGY**

This section describes the simulation framework used to solve this complex problem, including background assumptions and key equations. Assumptions impact travel behaviors (e.g., demand elasticities), EVCS owner costs (for land/space, equipment, operations and maintenance), and EVCS location options. Initial applications are for an entire day’s demand (to reflect all possible revenues). Analysis of more specific times of day will allow for greater congestion feedbacks but ignore demand that will impact profitability.

**Problem Setting**

U.S. PEV purchases rose to 1.1% of light-duty vehicle sales in 2016 (Richter, 2017). By March 2018, this share had increased to 1.6% of U.S. sales (EVAadoption, 2018). For this reason, PEVs are assumed to be 1.6% of total passenger vehicles on the Sioux Falls road network in this paper’s applications. But not everyone will want to charge while traveling intra-regionally.

Among PEVs, battery electric vehicles (BEVs) require charging (since BEVs cannot use gasoline). And BEV owners may choose to charge en route (rather than at one’s home or workplace or shopping destination, for example), like when traveling long distances (typically inter-regionally) or when forgetting to charge overnight (and possibly running out of charge that day). In contrast, plug-in hybrid electric vehicle (PHEV) owners may not care to wait to charge en route (since gasoline can be added quickly to PHEVs, generally with little to no circuity in one’s routing choice). Of course, hybrid electric vehicle (HEVs) cannot be plugged in and thus would not be charged en route. BEVs were two-thirds of all US PEV sales in 2016 (Statista, 2018), and perhaps one out of every 20 BEVs in use (5% of BEV users en route) will stop for charging within a city network (Hardman et al., 2018). Due to falling battery prices, rising climate change concerns, and other trends, PEV sales and BEV ownership levels are likely to continue rising, around the world. Moreover, shared self-driving or “autonomous” vehicle (SAV) fleets may be largely electric, giving rise to greater EVCS demand and station location solution needs (see, e.g., Loeb and Kockelman 2018).

PEV or BEV owners’ en-route station use and station selections will depend detour distances or travel times involved and queueing or wait times at desired charging stations. This work assumes that travelers are informed of congestion along all routes and at each EVCS, thanks to navigation technologies and charging-station broadcasts of queues. Random utility theory is used here for station choice: BEV users favor shortest total travel+charging time paths (from origin to final destination, recognizing delays to reach and while charging at EVCSs, for those who wish to charge en route that day). Of course, network congestion also affects network demand, for all travelers.
Charging station costs vary by cords provided and power rates delivered. Level 3 stations offer power levels from 20 to 50 kW, and thus can deliver 70 to 100 miles of passenger-car BEV range in 30 minutes or less. Smith and Castellano (2015) estimate Level 3 charging stations to cost $10,000 to $40,000 per charger and $2,300 to $6,000 for parts and labor in their installation, so those values are used here. Blink DC fast chargers were installed at an average price $22,626, and the lowest registered cost was $8,500 across 22 regions in U.S. (Idaho National Laboratory, 2015).

Different station sites carry different land costs, and some carry different energy costs (by rate of power delivery and high-voltage power-grid-access constraints. Here, land in the city center (1/3 of the 24 nodes) is assumed to cost $20,000 per station per year for a station of maximum three charging spot, while land elsewhere is assumed to be $10,000 per station, based US average land values of $510,000 per acre (Florida, 2017). Cord installation costs require labor, materials, permits and taxes, and assumed to cost $21,000 up front, per site. Variable costs include electric power fees, station maintenance, station signage, equipment updates, advertising and credit-card transaction fees. Electricity is assumed to cost 12 cents per kWh, or just $0.1 per minute of Level 3 charge time (assuming 30 minutes to provide over 24 kWh of charge, for 70 to 90 miles of driving range). Station owners may charge by the minute, like EVgo does (20¢/minute charge across many states in U.S.) or per visit (like Blink is doing, at $7 to $10, and AeroVironment is doing, at $7.50 per session) (Berman, 2018). Credit card transaction costs are assumed to be 5% of the fee. The average charging time is assumed to be 30 minutes here, but may vary from 10 to 60 minutes or more, depending on customer needs and pricing structure used. Other owner costs, as described above, are assumed to be $10,000 per station per year.

Charging stations can be located at any of the network’s nodes (just 24 in this initial application). For the Sioux Falls network, these 24 nodes are also origins and destinations of the region’s the 3.6 million vehicle-trips each day (rather than having separate zone centroids that connect to the network). If an origin-destination pair requires a BEV user to travel further to the EVCS than one would travel to go directly to the destination, the BEV will decide not to charge en route.

On-site power supply is an important consideration for EVCS owners. Direct-current fast-charging (DCFC) or super-charging and hyper-charging (like 24 mi/20 minutes at 24kW, 50 mi/20 minutes at 50kW and 90mi/20minutes at 90kW with 208/480VAC 3-phase charger) generally require relatively big batteries on site, to avoid overtaxing the grid (and causing brownouts) – and to avoid very high power pricing (by grid managers) (Smith and Castellano, 2015). Putrus et al. (2009) investigated the impacts of PEV charging on power distribution networks in the US that heavy PEV deployment and peak charging can create power-delivery issues for existing power networks, including voltage imbalance and transformer loss. The situation can be ameliorated if fast-charge stations are reasonably distributed across the grid, relative to power generation and transmission stations. Bullis (2013) argues that public fast-charging stations for cars and trucks should not impact the grid much because our commercial grids have transformers and other equipment sized to accommodate large loads, for big businesses, apartment buildings, and so forth. To avoid excessive power demand in any one location, a maximum cord count of 3 is assumed at each station.

Queues may still be observed at a station. Since static traffic and station assignment algorithms are used here (assuming stationing demand and supply conditions for network links and station cords), BEV users beyond 80% of any EVCS’s capacity are assumed to wait some period of time for a charging cord or space to become available. Any EVCS demand levels that exceed station capacity are not able to charge their vehicles, so such revenues are lost.

### Problem Formulation

Using the above assumptions and ideas, the profit-maximization problem for charging station provision across a town, city or region can be stated as follows:
\[
\max_y \left( \sum_{(r,v) \in Z^2} d_r^v (p_e - p_v) - f_m - \sum_{\forall v \in V} f_v y_v \right) T - \sum_{\forall v \in V} N_v f_v^v y_v
\]

s.t.  
\[y_v = \{0,1\} \quad \forall v \in V\]  
\[d_r^v = d_r^v + d_r^v + d_r^v \quad \forall (r,v) \in Z^2\]  
\[N_v = \min \left\{ \frac{\sum_{\forall v \in V} d_r^v}{S}, M \right\} \quad \forall v \in V\]  
\[\sum_{\forall v \in V} d_r^v = N_v S \quad \forall v \in V\]

where \[d_r^v = \arg \min_{i,h,d} \sum_{(i,j) \in A} \int_{t_d} t_j (x) dx - \sum_{(r,s) \in Z^2} \int_0^d d_r^v D^{-1}(\omega) d\omega \quad \forall (r,v) \in Z^2\]

s.t.  
\[x_j = \sum_{\pi \in \Pi} h_d \delta_d^j \quad \forall (i,j) \in A\]  
\[\sum_{\pi \in \Pi} h_d = d_r^v \quad \forall (r,s) \in Z^2\]  
\[h_d \geq 0 \quad \forall \pi \in \Pi\]  
\[d_r^v \geq 0 \quad \forall (r,s) \in Z^2\]

In this formulation, \(Z\) is the travel demand matrix of all travelers, \(T\) is the time horizon, \(A\) is the set of directed links in the road network, \(\Pi\) is the set of all used paths (for all OD pairs) in the network, \(V\) is the set of nodes in the network (just 24 for the Sioux Falls network), \(h_d\) is the flow of travelers choosing path \(\pi\), \(D\) is the demand function for each OD pair (based on shortest-path travel times), \(x_j\) is the vehicle flow on link \((i,j)\), and \(t_j(x)\) is the travel time performance function for link \((i,j)\) at flow level \(x\).

Equations (1) to (5) are the facility location portion of this EVCS problem. Equation (1) is the profit function of the EVCS owners, and thus the sum of revenues collected from BEV owners that decide to stop and charge their vehicles, minus all other costs (for site rental, equipment provision, operations, and maintenance). \(t\) is the analysis time horizon of the investment of building EVCS (e.g., 3 years in the initial Sioux Falls application), \(\epsilon\) is the share of revenues that owners keep after credit card fee, \(p\) is the price or fee paid by BEV owners that charge at a station en route, \(p_v\) is the price of electricity per vehicle charged (10ct/min x 30 min/vehicle charge = $3/vehicle), \(f_v\) is the fixed price of each cord (and its installation), \(f_v\) is the land or site fees per year per station (much like a mortgage payment), \(f_m\) is annual station maintenance cost, \(d_r^v\) is the supply of BEVs from node \(r\) to node \(v\) (i.e., vehicles that seek to charge their batteries after considering a path’s EVCS total travel time situation), \(S\) is the daily flow a cord can serve, and \(N_v\) is the number of cords ultimately provided at station \(v\). The \(N_vS\) is the final capacity of a station that can serve daily at node \(v\).

The key decision variables are the indicators \(y_v\), in Eq. (2): \(y_v = 1\) when node \(v\) is used/chosen for an EVCS, and 0 otherwise. Another set of decision variables \(d_r^v\) are the modified demands from nodes \(r\) to nodes \(s\). These are obtained via the network updating process, which returns the OD matrices for both BEVs who would need to charge en route \((d_r^v + d_r^v\) and those do not \((d_r^v\), which consist of conventional vehicles, BEVs that do not want to charge and BEVs that would like to charge but decide it’s too time-consuming to charge en route. BEVs who would need to charge en route can charge at
origins or destinations when the corresponding origin or destination is opened as a charging station. The number of cords provided at each EVCS ($N_v$) is also an important decision variable.

Eq. (3) updates and adjusts network trip tables to reflect EVCS use, with the station choice incorporated: $d^{rv}$ is the demand by conventional vehicles from origin $r$ to destination $s$, $d^{rv}_c$ is the demand of BEVs from origin $r$ to destination $s$, and $d^{vs}_c$ is the demand of BEVs from station $v'$ to destination $s$. The demand matrix obtained in Eq. (3) is used for the traffic assignment procedure.

Eqs. (6) through (10) solve the user-equilibrium traffic assignment problem with elastic demand and EVCSs present in the network. Their solution delivers link flows and path demands, which are used as inputs to the overall problem’s primary objective function: BEVs that stop to charge en route impact Eq. (1) - the profit equation. Based on Eq. (6)’s BEV charging demands, optimal station cord counts are determined. Cord counts are also limited by station sizing (which is assumed fixed here, but can be varied in an expanded formulation), and the maximum (due to size or demand) is shown in constraint Eq. (4). The optimal cord-count decision values (which maximize EVCS owner profits) are shown in Eq. (5), as $N_v$ values.

Travelers are permitted to shift to other modes (or destinations or curtail trip-making altogether) when congestion increases. Thus, demand between each OD pair is elastic, as a function of that OD pair’s shortest-path travel time. Sheffi’s (1985) exponential demand function is used here, as follows:

$$D_{rs} = D^0_{rs} \times e^{-\alpha (\beta^{rs}_{u,v} + \beta^{rs}_{l,v})}$$

Here, $t_{rs}$ is the shortest path travel time from origin $r$ to destination $s$, $l_{rs}$ is the shortest-path distance between $r$ and $s$, $\beta^{rs}_v$ is vehicle operating cost per mile (40 ct/mile), and $\beta^{rs}_v = \beta^{rs}_v \times VOTT$ is the cost of shortest-path travel time, $u_{rs}$, where the value of travel time ($VOTT$) is assumed to be $10$/hour. A values of $\alpha = -0.01$ is used here so that demand is not too elastic with respect to travel time and distance; a more accurate calibration of this $\alpha$ value can deliver more realistic results.

**EVCS SOLUTION**

This section provides the solution methods to the NP-hard facility location problem. The overall problem is solved using a genetic algorithm (GA) approach, and a modified Frank-Wolfe algorithm is used to solve the traffic assignment portion. A station-choice algorithm is also introduced to handle the EVCS choice of the BEV users.

**Genetic Algorithm**

A GA is a metaheuristic for (approximately) solving complex optimization problems, inspired by the process of natural selection (Mitchell, 1998). GAs rely on bio-inspired operators, including mutation, crossover, and selection across decision variables’ values. Here, the GA solution is a combination of the network’s node values (0’s and 1’s), indicating which nodes will be selected to host EVCSs. One updates each generation of solutions by selecting the best solutions (those delivering higher profit levels) from earlier generations, and randomly mutating some values from 0 to 1 or from 1 to 0, or crossing over/exchanging a section of one set of binary values with another, in current-solution vectors. Each iteration’s suggestion of EVCS locations results in an updated traffic assignment (reflecting user equilibrium with elastic demand) and an updated cord count recommendation (to maximize profits, given current station locations). The stopping criterion used here is 100 iterations, due to the significant computational load (about 20 minutes per iteration, including 80 traffic assignments), and Figure 1 illustrates the solution process. The design of the stations as well as their locations are determined by the best solution among these 100 iterations.
FIGURE 1 Genetic algorithm process used

Here, GA parameters are determined after testing a few sets of parameters to obtain a reasonable computation speed while ensuring the accuracy. The GA population consists of 8 EVCS assignment sets, and thus each GA iteration relies on 8 different traffic assignment solutions. The selection rate assumption used is 0.5, implying that 4 solutions are used to generate 4 solutions after crossover. All binary elements of these 8 solutions have a probability of 0.05 to mutate from 0 to 1 or from 1 to 0.

Traffic Assignment Algorithm
Static traffic assignment is a traditional network problem (Sheffi, 1985). It seeks a user equilibrium (UE) so that minimum travel time paths are achieved for travelers between all OD pairs (Wardrop, 1952). The Frank-Wolfe algorithm is used here, and both those seeking to charge BEVs en route and those not seeking to charge are assigned simultaneously. The relative gap used here, as the stop criteria for convergence, is set to 0.0001. Smaller values will enable clearer convergence, but computing demands on supercomputers will limit this choice.

Station Choice Algorithm
Equilibrium network flows can shift a fair bit, at least for BEV owners seeking to charge en route, due to different EVCS siting decisions. Those who stop to charge en route create two sub-trip tables, from origin to EVCS and from EVCS to final destination. Station choice happens for those trips who share the same
OD pair \((r, s)\). EVCS choice for station \(v'\) among all potential station \(V\) is determined using a logit choice model:

\[
d_{c}^{rv} = d_{c}^{rs} = \frac{\exp(t_{rv} + t_{vs} + \rho \times w_{v})}{\sum_{v} \exp(t_{rv} + t_{vs} + \rho \times w_{v})} \quad \forall (r, s) \in Z^2, \forall v \in V
\]

where \(d_{c}^{rv}\) is the demand of BEV users (who need to charge en route) who travel from origin \(r\) to station \(v'\) to charge for a trip from origin \(r\) to destination \(s\), which equals to the demand \(d_{c}^{rs}\) from station \(v'\) to destination \(s\), \(t_{rv}\) and \(t_{vs}\) are the congested travel time from origin \(r\) to station \(v'\) and from station \(v'\) to destination \(s\), respectively, \(w_{v}\) is expected/average wait time at station \(v\), and \(\rho\) is the relative importance of wait time (in proportion to travel time). Therefore, an EVCS choice depends on the detour time \((t_{rv} + t_{vs})\) and the waiting time at the station. The total demand arriving at a station \(v'\) is

\[
\sum_{(r,s)\in Z^2} d_{c}^{rv}
\]

For each EVCS siting decision (as given by the GA described above), traffic assignment is first conducted, and then EVCS wait times are ascertained. Station wait times impact EVCS choices by those wishing to charge their BEVs en route. Another procedure is conducted to obtain a stable solution of station choice: under the EVCS patterns, people would no longer shift their station choice, considering the congestion at the stations. The updated flows to each EVCS are a convex combination of prior BEV assignments to EVCSs and the newest set of assignments, using the method of successive averages:

\[
d_{c}^{rv} = \frac{1}{\gamma} \times d_{c,new}^{rv} + \frac{\gamma - 1}{\gamma} \times d_{c,old}^{rv} \quad \forall (r, v) \in Z^2, \gamma = 2, 3, 4 \ldots,
\]

\[
d_{c}^{rs} = \frac{1}{\gamma} \times d_{c,new}^{rs} + \frac{\gamma - 1}{\gamma} \times d_{c,old}^{rs} \quad \forall (r, v) \in Z^2, \gamma = 2, 3, 4 \ldots,
\]

The procedure should iterate until assignments of BEV users to EVCS sites are stable. However, since there also is a traffic assignment procedure running alongside, this calculation is run just 10 times, to obtain a relatively stable pattern of station assignments to BEV users, while speeding up the long computing times.

**SCENARIO TEST**

**Data Input**

The Sioux Falls’ network data were developed by LeBlanc et al. (1975), with 24 nodes and 76 links, as shown in Figure 2. The OD matrix contains 3.6 million vehicle-trips per day. The Bureau of Public Roads (TRB, 2000) link-performance function is used here \((t = t_{0} \ast \left(1 + \alpha \ast \left(\frac{v}{c}\right)^{\beta}\right)\). where \(v\) is the traffic volume, \(c\) is the capacity, \(t_{0}\) is the free flow travel time, \(\alpha\) and \(\beta\) are empirical coefficients), with parameters \(\alpha = 0.84\) and \(\beta = 5.5\), to reflect a true capacity values.
Scenarios Analyzed

Of course, different cost and behavioral settings will generally deliver different EVCS siting and sizing decisions. Table 1 describes the various levels of key assumptions used to define the 15 distinctive scenarios tested here. The variety in these settings allow one to examine how BEV owners’ demand levels and EVCS owners’ costs, fee choices, cord count constraints, and time horizons should impact decision-making, and to ascertain whether there is some meaningful stability or robustness in profit-maximizing decisions. As shown in Table 2, Table 1’s Level 2 values are pivoted off of, as a Base Case, to provide 15 scenarios total (by testing values shown in Table 1’s Level 1 and 3 columns).

**TABLE 1 Scenario Design Settings**

<table>
<thead>
<tr>
<th></th>
<th>Level 1</th>
<th>Level 2 (Base Case)</th>
<th>Level 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time horizon (years)</td>
<td>2 yr</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>Max cord # per station</td>
<td>1 cord</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>Charging time (minutes)</td>
<td>20 min</td>
<td>30</td>
<td>40</td>
</tr>
<tr>
<td>Fee per charge ($)</td>
<td>$6/charge</td>
<td>8</td>
<td>10</td>
</tr>
<tr>
<td>%BEV users needing to charge</td>
<td>5% of BEVs</td>
<td>10%</td>
<td>100%</td>
</tr>
</tbody>
</table>

**EVCS Siting and Design Results**

Table 2 shows the results of these 15 scenarios. Total number of stations developed (to maximize EVCS investor profits) ranges from 8 to all 24 of this coarse network’s nodes. The typical investment decision is a rather reliable 17 sites, representing a spatially-extensive investment. However, with a less coarse network (i.e., a greater number of nodes) and more fixed costs in setting up each site (and no constraints on expanding each site), a much lower ratio of sites per network node is expected to be optimal (e.g., 1 to 10% of nodes, rather than 33 to 100% and averaging about 70%).

Different scenarios can be compared to the base case, which is shown in Table 2’s secondrow. The base case is defined as allowing no more than two cords per station, assuming a 30-minute charge time, and
carrying an $8$ fee for each BEV charging event, over a 3-year investment period with 10% of BEV owners hoping to charge en route. With a longer (or shorter) time horizon, profits rise (or fall) roughly $0.5$ million per year for this very specific network case. There are no queues expected in this static assignment setup under these first 3 scenarios (3-year base case tested with 2- and 4-year periods), assuming EVCS demand remains stable over time. However, PEV and BEV ownership levels are growing, most everywhere in the world (Schefer and Knox, 2018; Kiser et al., 2018). With increasing BEV use, especially by those who do not have good charging options at home or work or school, queues can emerge, and 2 or 3 cords per station may inadequate, especially at central stations, in more complex and realistic networks, where relatively few nodes are assigned an EVCS. Fortunately, advances in power delivery and on-site battery storage may also increase power delivery rates, thereby reducing charging durations for similar range delivery. The algorithms developed here can handle such settings, assuming computing power exists for those cases.

If no more than one cord can be provide at each station, queues are expected at many stations and times of day, averaging 13.4 BEVs, stifling profitability. Allowing 3 cords per station results in fewer EVCS sites needed. Queues also emerge if one alters the base case scenario to have 40 minute charging times. Longer turnover between BEV customers results in lower revenues and profits (assuming the same fee is used, per charging event).

Of course, fee or pricing decisions also affect station siting and sizing decisions. Higher fees lead to more stations being opened across the network and more cords being added to many sites, to maximize EVCS owner profits. A fare of $6 per charge is not enough to return positive profits, and also results in queuing at many stations. More BEV owners deciding to charge en route, combined with rather low caps on cord counts, delivers more queues, but also a healthy return on investment.

<table>
<thead>
<tr>
<th>Time Horizon (years)</th>
<th>Max # Cords</th>
<th>Charging Time (minutes/charge)</th>
<th>Fee ($ per charge)</th>
<th>% BEV Owners Seeking Charge En Route</th>
<th>Profits ($ Million)</th>
<th># Queued BEVs Expected Per Day</th>
<th>Total Cords</th>
<th># Stations</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 yrs</td>
<td>2 cords</td>
<td>30 min</td>
<td>$8/charge</td>
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<td>0 BEVs</td>
<td>24 cords</td>
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<td>17</td>
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<td>11</td>
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<td>1.97</td>
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<td>0.15</td>
<td>11.7</td>
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<td>30</td>
<td>8</td>
<td>5%</td>
<td>0.66</td>
<td>0</td>
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<td>13</td>
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<td>100%</td>
<td>5.06</td>
<td>381.1</td>
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</table>

Table 3 specifies the profit-maximizing nodes chosen for EVCSs – by listing their cord counts. Nodes not assigned a station or cords are denoted “-". Important spatial patterns can be seen when combining these values with Figure 2’s network. For example, when cord count can be as high as three, only nodes 10 (at the city’s center) and 20 (on the southeast corner of the network, which near highway with a park there)
merit this kind of capacity, while the optimal station count falls by 5. Essentially, if power supply (and site space) permits, several stations with several cords can profitably compensate for many fewer station sites (though BEV owners may not prefer such setups, due to longer detours to arrive at an EVCS). Stations 11 and 16 consistently play important roles, while nodes 6 and 23 are less relevant. Interstate Highway 29 has nodes 1, 3, 12 and 13 as major interchanges, with each consistently receiving a station (though not always with maximum cord counts). If a larger region and external trips had been permitted, station and cord counts on such perimeter highways would presumably rise.

As expected, longer charging times and higher shares of BEVs seeking to charge en route result in more cords or stations being provided. Interestingly, three cords seem like a common investment decision, given that year US Department of Energy (2018) statistics for year 2018 suggest that the US has 51,766 charging outlets (all types of electric vehicle chargers) across 18,489 public charging stations (thus averaging 2.8 cords per station). Of course, most of those are not Level 3 or DCFC charging stations, but many may eventually upgrade. Maximum profits appear to emerge under longer time horizons with more cords permitted. Of course, competition is always a possibility, and a single owner is unlikely to control all sites.

### TABLE 3. Optimal Cord Counts by Network Node (EVCS Site) across 15 Scenarios

<table>
<thead>
<tr>
<th>Station Index (Fig. 2)</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
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<td>Time Horizon (years)</td>
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<td>2</td>
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<td>1</td>
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<tr>
<td>Max # Cords</td>
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<tr>
<td>Charging Time (min per charge)</td>
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<tr>
<td>Fare ($ per charge)</td>
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<td>1</td>
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<tr>
<td>% BEV Users seeking charge</td>
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<td>1</td>
<td>0</td>
<td>0</td>
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<td>Charging Time (min per charge)</td>
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<tr>
<td>% BEV Users seeking charge</td>
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### CONCLUSIONS

This work design, applies, and iteratively solves a complex charging station location-and-sizing problem to maximize EVCS owner profits across a region for PEV owners who wish to charge en route. The model is the first to allow for congested-travel and congested-station feedback into travelers’ route choices and BEV owners’ station choices, as well as elastic demand for all road users (BEVs and non-BEVs). The method’s results deliver specific station locations and cord-count details, while reflecting all Level 3 charging station costs. The Sioux Falls application results suggest that profit-maximizing EVCS sites are generally located largely in the city center and alongside major highways. When assuming that 10% of the town’s PEV users (or just 0.16% of all vehicle-trips) will seek en-route charging, a 30-minute charging fee of $6 is not enough to deliver a profit in 3 years time (with power-delivery costs of 12¢/kWh, land rental costs of $10,000 per station per year, and O&M costs of $10,000 per station per year). In contrast, $8 and $10 charging fees deliver reasonable profits. Providing no more than 2 cords at each station can accommodate most PEV owner demands for en-route charging, but lowers EVCS profitability. Profits rise when operators take a longer-term perspective, but this complicates the solution, requiring...
longer computing times (on fast supercomputers). Shorter charging sessions, higher fees, and/or allowing for more cords per site also increase profits, everything else constant.

Enhancements to this work may include calibration of the demand-elasticity parameter and wait-time (at charging stations) disutility, through survey work and actual station use and queuing observations. A much larger network application would also be helpful, with station counts limited and station location costs much more variable over space and position. However, for larger, more realistic applications, faster algorithms will key to achieving profit-maximizing user equilibria in reasonable computing times. Improved UE algorithms could be path-based (Jayakrishnan et al., 1994) or bush-based (Dial, 1971), as they track paths or bushes instead of links in the algorithm. The GA-solution assumptions and parameters used here may also be improved through machine learning techniques. Site specific variations will also exist, on power delivery rates and costs, land rental and site maintenance costs, and cord supply costs. And pricing or fees may work best per minute and per kWh delivered, further complicating the solution process. Finally, not all PEVs can use the same charging facilities yet - due to cross-manufacturer design incompatibilities. Currently, nearly all BEVs that offer DCFC capability in the U.S. use one of three standards: CHAdeMO, Combined Charging System (CCS), or a Tesla Supercharger. Experts expect that all three standards will continue coexisting in the U.S. and many other places (McDonald, 2016). Interoperability, for maximum demand uptake at EVCS sites, may require more investment expense than assumed here, especially if one wishes to reduce charging durations to become more competitive with conventional vehicle refueling. Fortunately, technologists are tackling such issues, and prices continue to fall, making EV futures more and more likely.

AUTHOR CONTRIBUTION STATEMENT
The authors confirm the contribution to the paper as follows: study conception and design: Huang, Y.; analysis and interpretation of results: Huang, Y. and Kockelman, K.; draft manuscript preparation: Huang, Y., Kockelman, K. All authors reviewed the results and approved the final version of the manuscript.

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